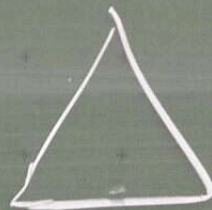


NOR

NAND

OR

AND



NOT



#GAMES =

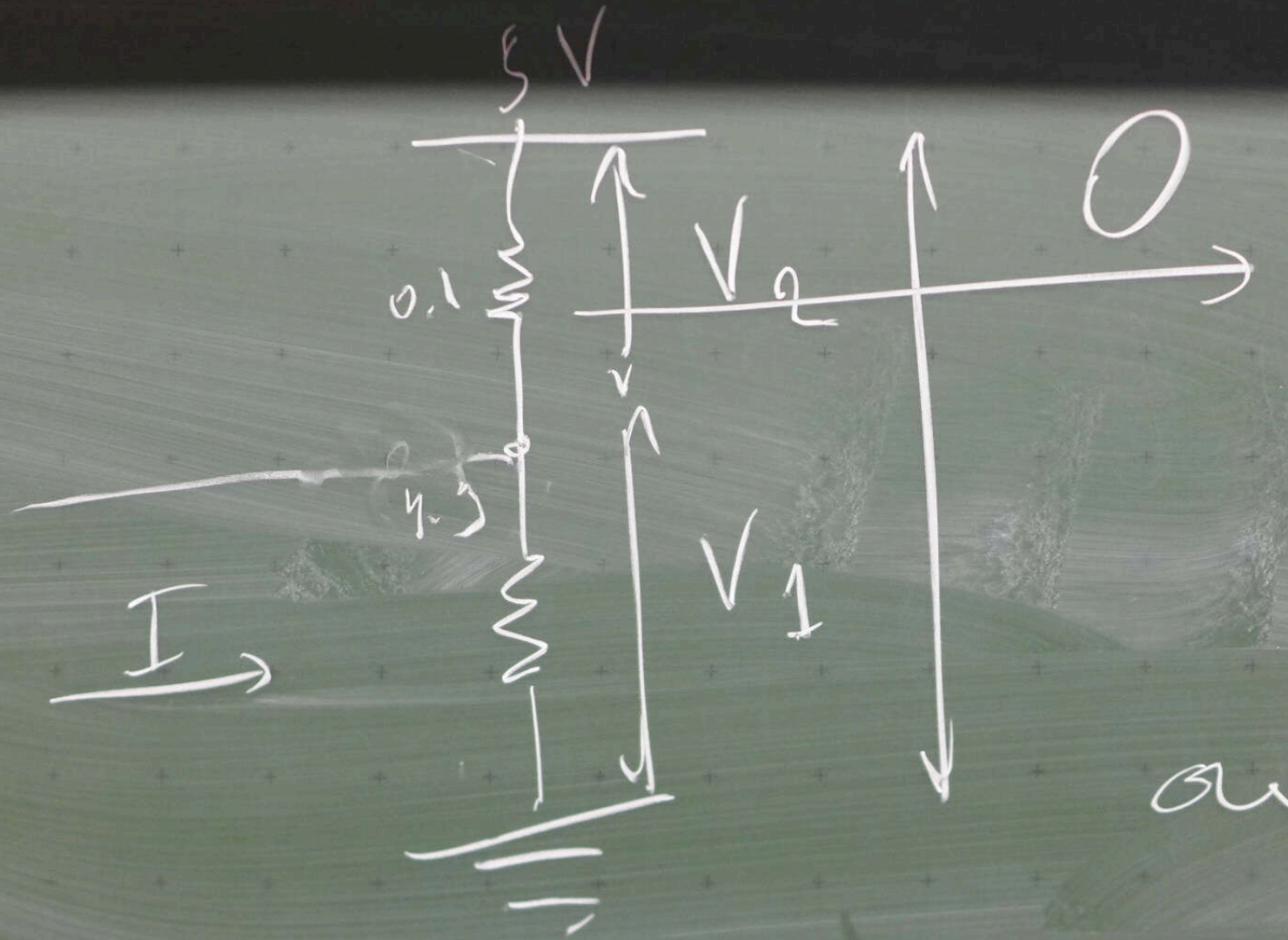
AND
2 I

+

OR
0

$$\text{out}_1 = (\text{in}_1 \cdot \text{in}_2) + (\text{in}_3 \cdot 1)$$

$$= (\text{in}_1 + \text{in}_3) \cdot (\text{in}_2 + 1)$$



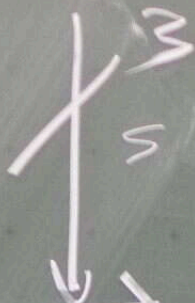
$$\left[1 + 1 \right] =$$

BOOLEAN

1

N

2



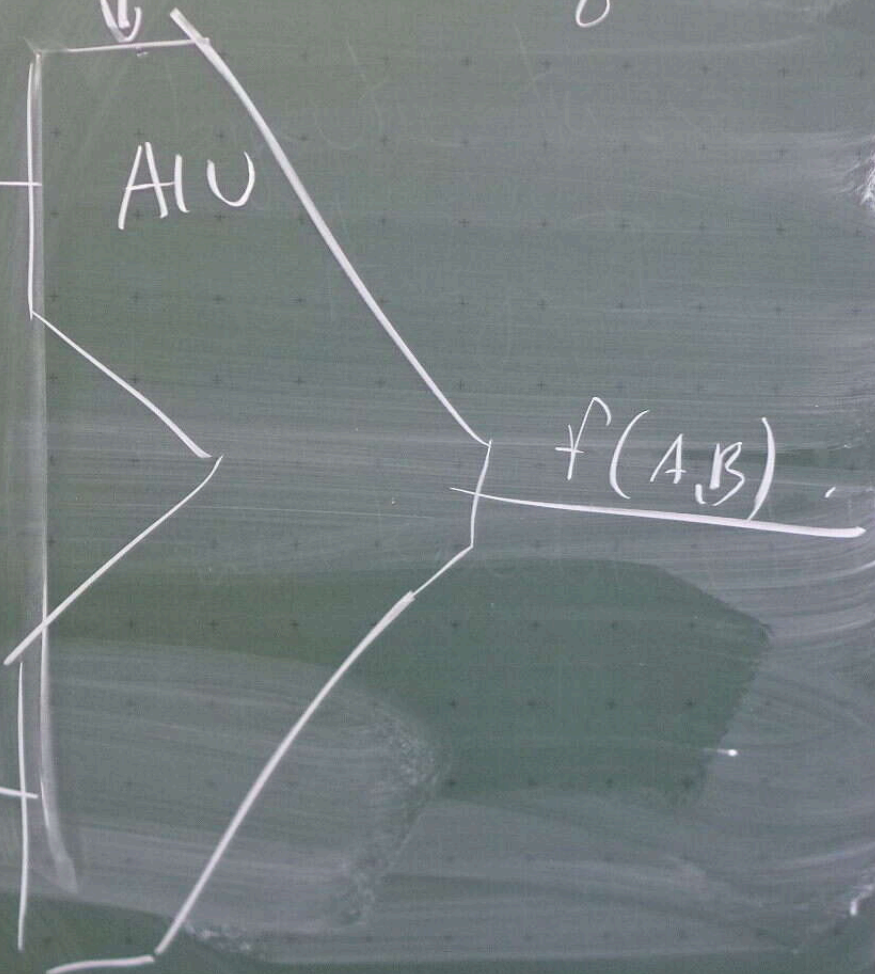
8

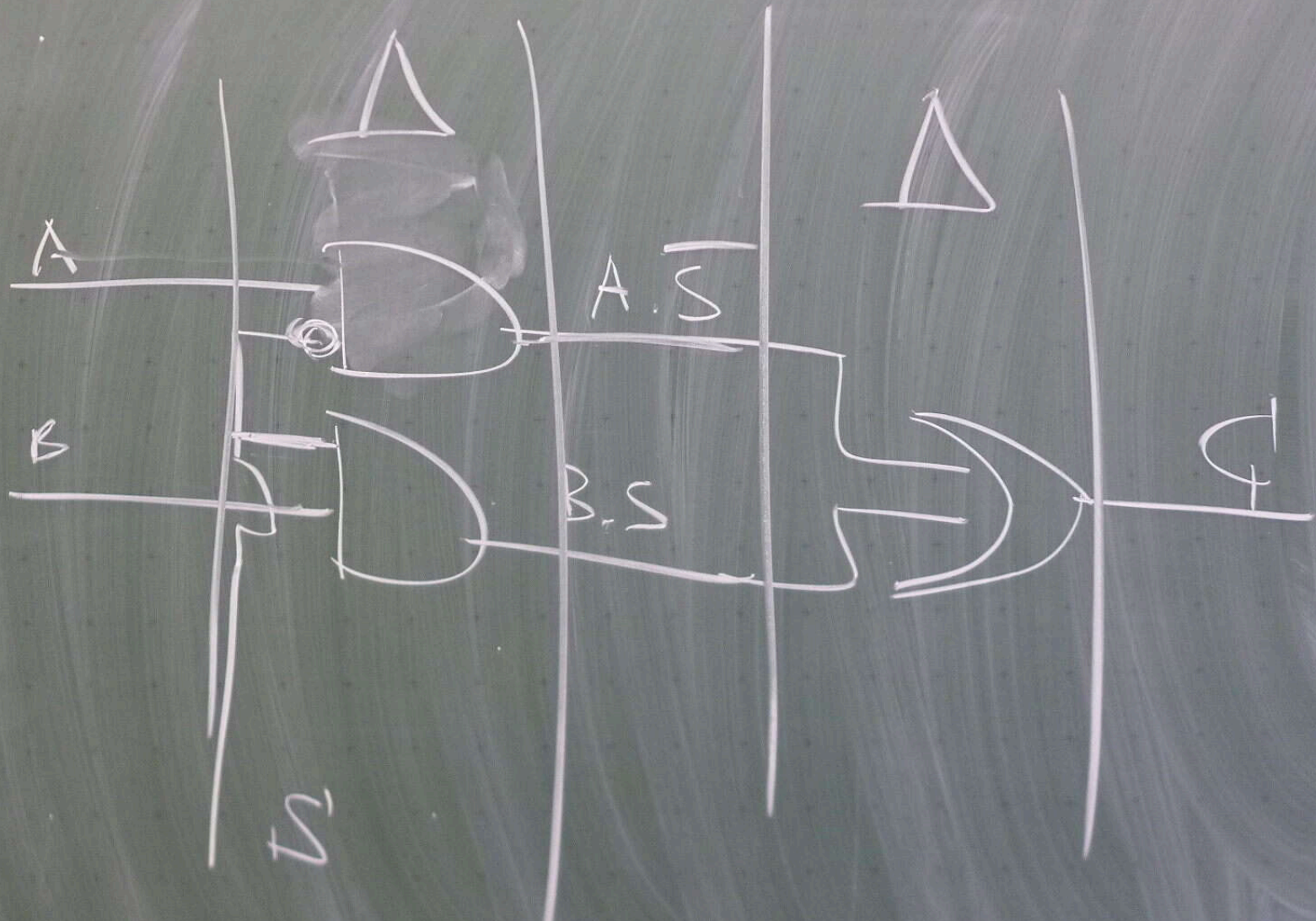
~~A 32~~

AIU

$f(A, B)$

~~B 32~~





#GATES =

2

I = 64

+

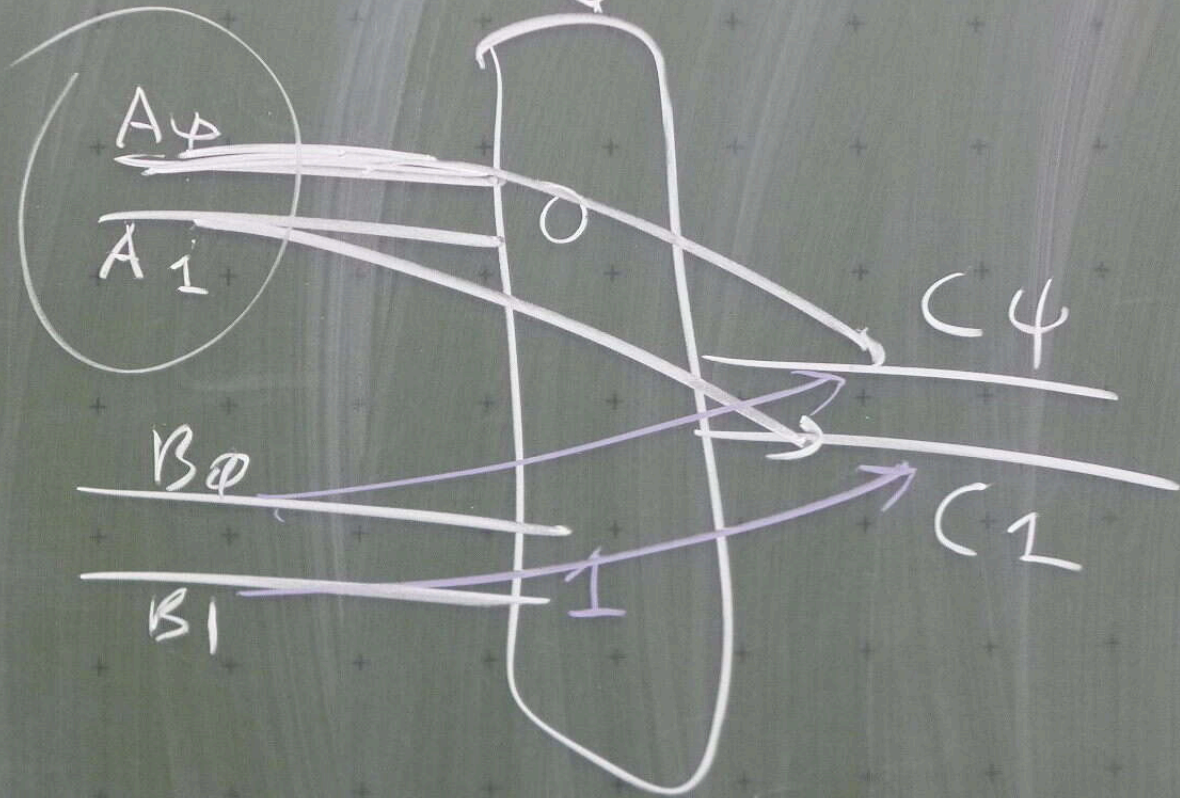
O = 32

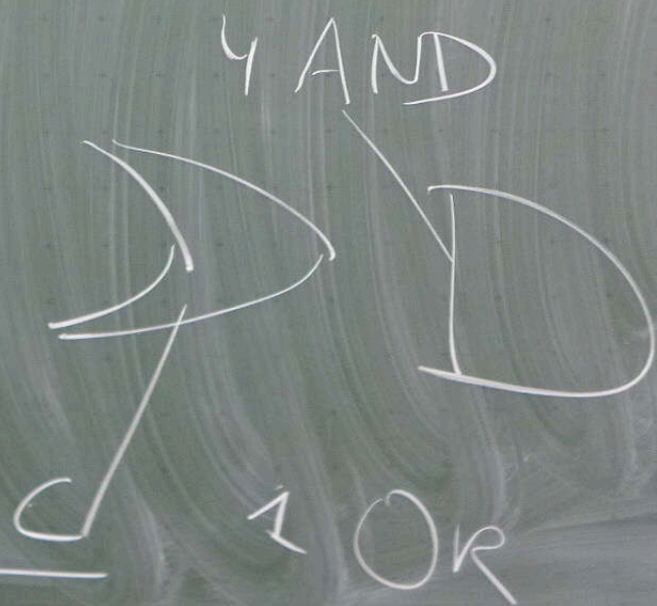
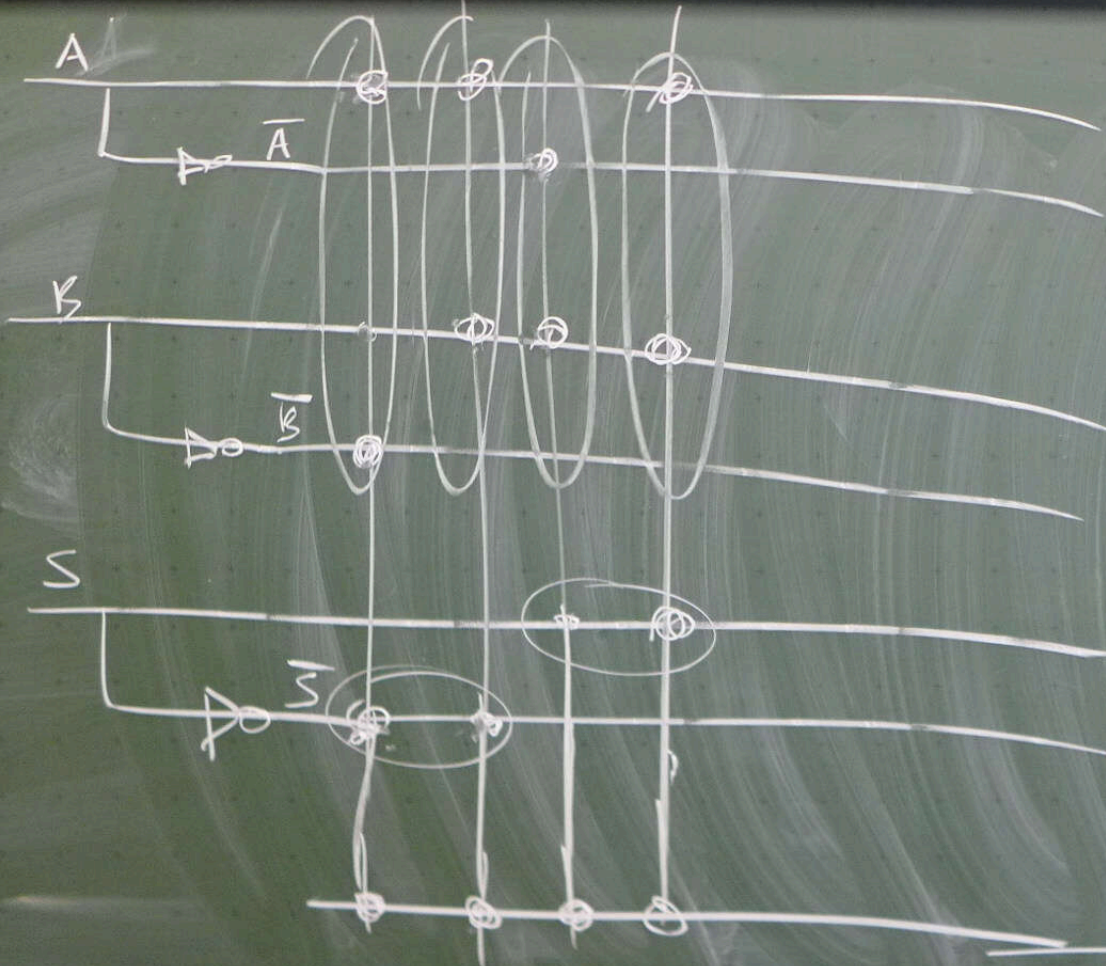
A

32

~~A 2~~

~~B 2~~



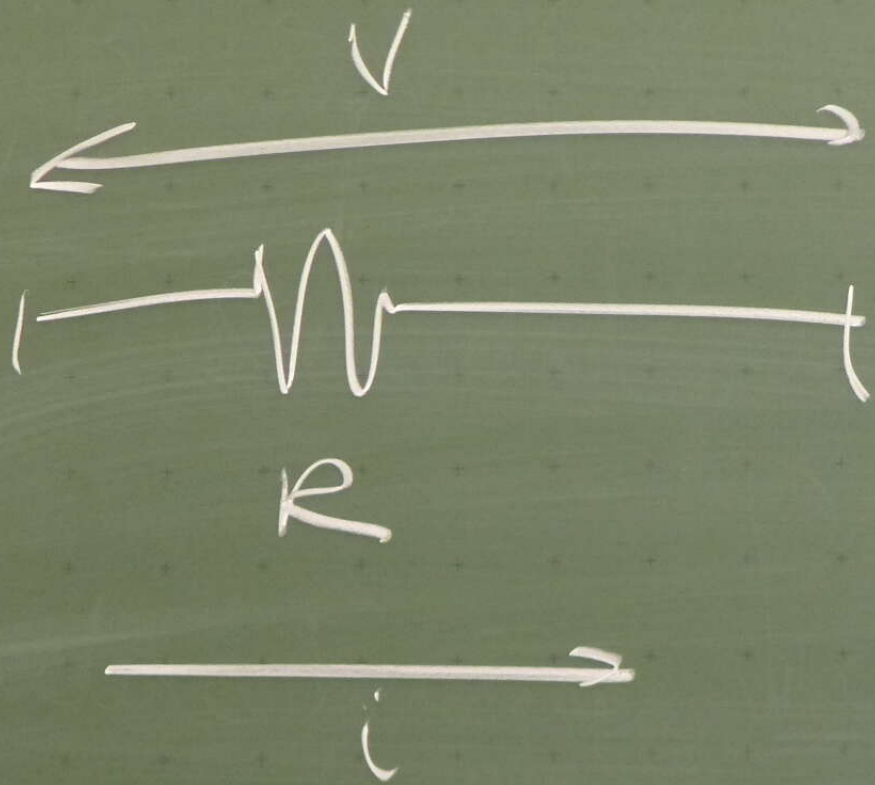


$$\overline{S} \cdot (A\overline{B} + \overline{S}A \cdot B) + S \cdot (\overline{A} \cdot B + SA \cdot B)$$

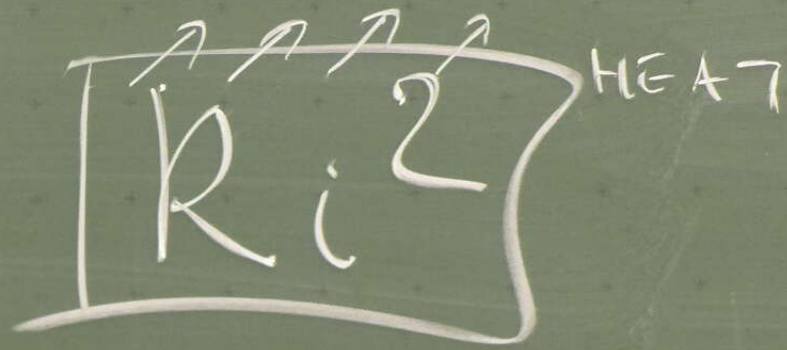
$$\overline{S} \cdot (A\overline{B} + A \cdot B) + S \cdot (\overline{A} \cdot B + A \cdot B)$$

$$\overline{S} \cdot A \cdot (\overline{B} + B) + S \cdot B (\overline{A} + A)$$

1 1



$$V = Ri$$



(Supp)

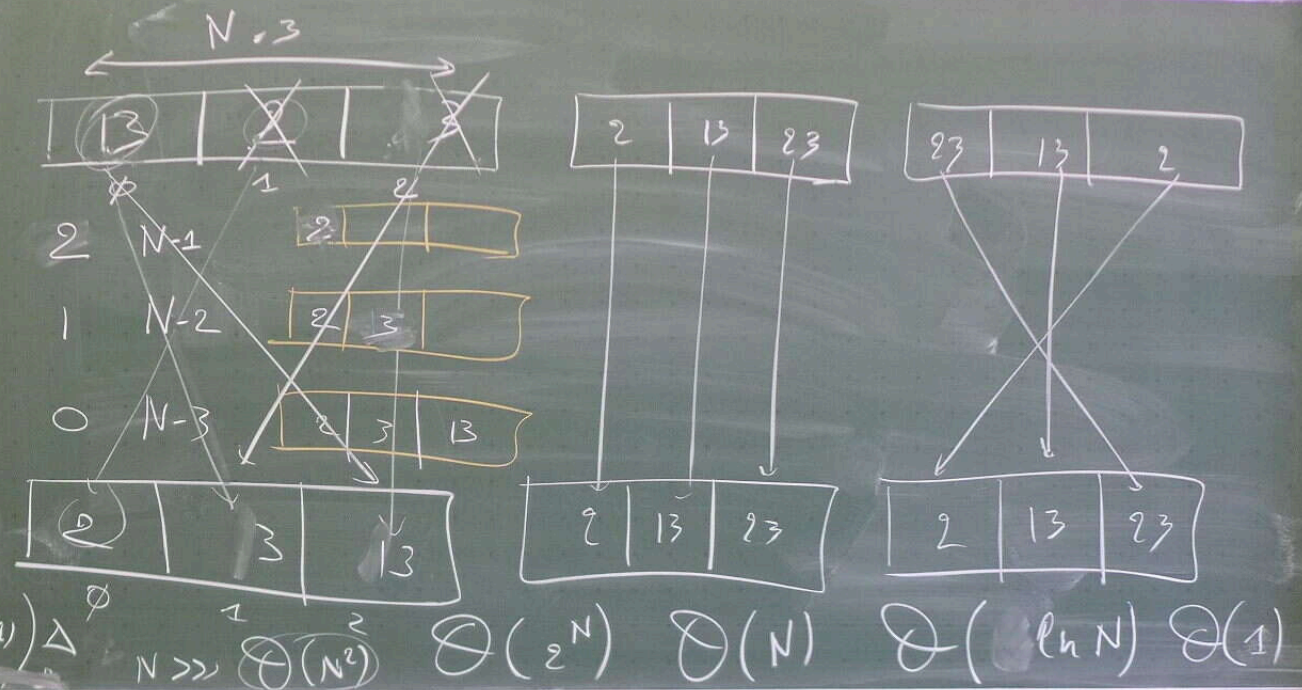
IMPLEMENTED
 SORTING
 PROGRAMS ALGORITHM

$$t(x \leq y) = \Delta$$

COMPLEXITY $\sim \Delta$

$$\text{COMPLEXITY} = 0 + 1 + 2 + 3 + \dots + (N-2) + (N-1) \Delta$$

$$= \frac{N(N-1)}{2} \Delta = \frac{N^2 - N}{2} \Delta$$



$$1 + 2 + \dots + (N-1) + N = \frac{N(N+1)}{2}$$

$$1 + 2 + \dots + (N-1) = \frac{(N-1)N}{2}$$

(Tijds) PERFORMANTIE

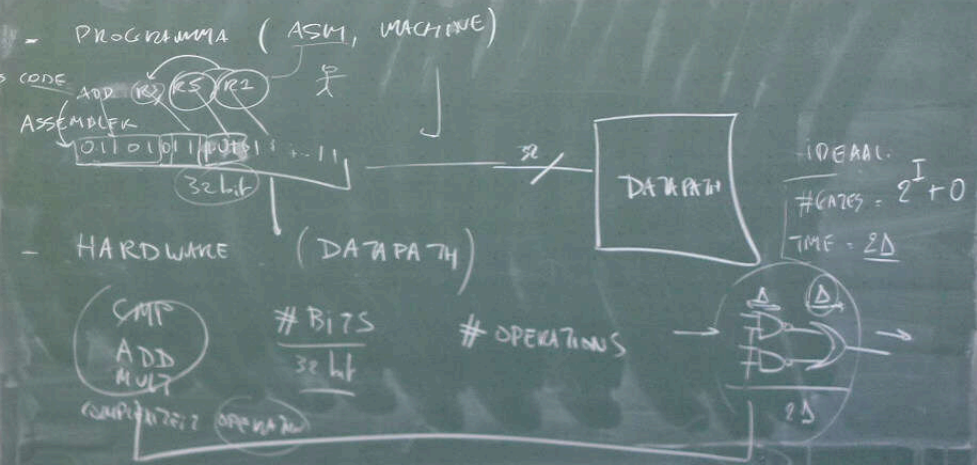
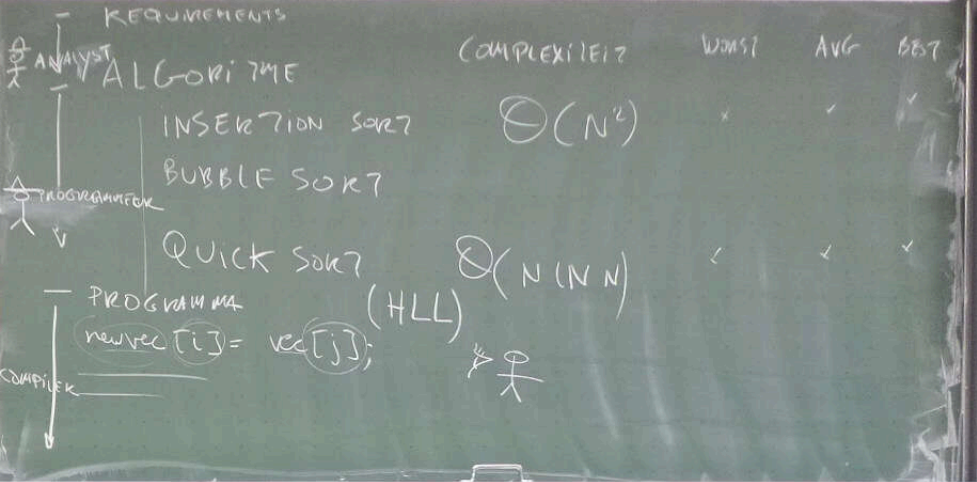


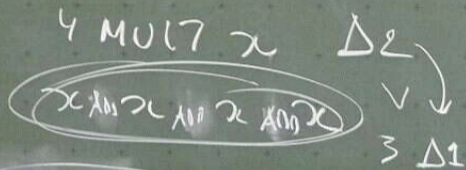
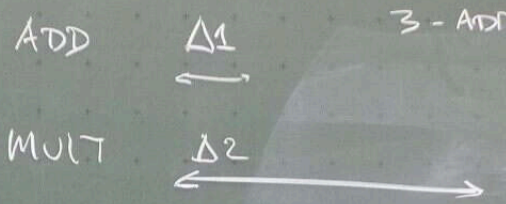
=

lengte
tijdsduur

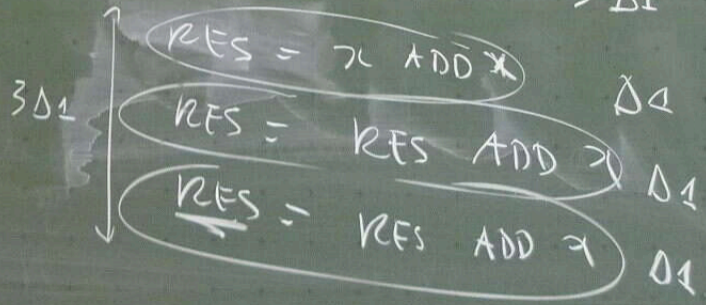
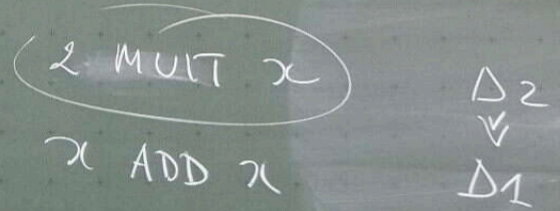
$$\frac{1}{\text{tijdsduur}}$$



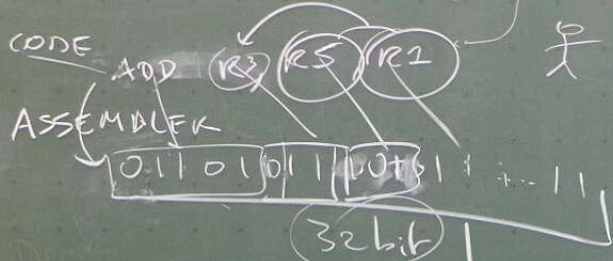




OPTIMIZING
 COMPILER \curvearrowright



PROGRAMMA (ASM, MACHINE)



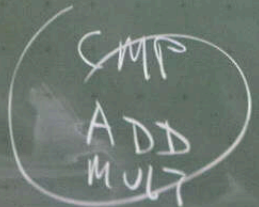
HARDWARE (DATA PATH)



IDEAL:

#GATES = $2^I + O$

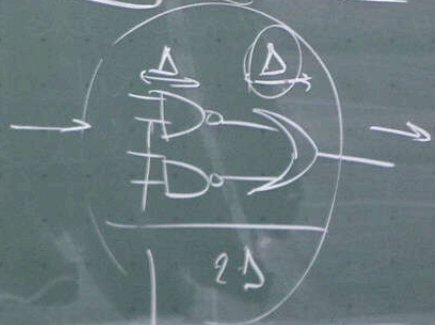
TIME = 2Δ



BITS

32 bit

OPERATIONS



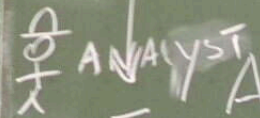
COMPLEXITÄT: OPERATION

Δ2

↓

Δ1

REQUIREMENTS



ALGORITHM

INSERTION SORT

COMPLEXITEIT

WORST

AVG

BEST

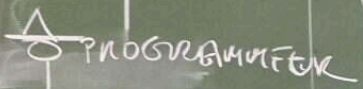
$O(N^2)$

x

✓

✓

BUBBLE SORT



QUICK SORT

$O(N(NN))$

✓

✓

✓

PROGRAMMA

(HLL)

newvec [i] = vec [j];



COMPILER



~~PROGRAM (III)~~

~~SUM = 0~~

~~FOR CTR IN 0..5:~~ (IV-1)

~~SUM = SUM + CTR~~

(SUM += CTR)

LOC = 4

~~while True:~~

~~PASS~~

loc = 2

$$\text{SUM} = \phi$$

$$\text{CTR} = \phi$$

$$\text{SUM} = \text{SUM} + \text{CTR}$$



$$\text{CTR} = 1$$

$$\text{SUM} = \text{SUM} + \text{CTR}$$

$$\text{CTR} = 2$$



INSTRUCTIONS

$$2 \times 1\phi + 1 = 21$$

$$2 \times N + 1 \quad \dots$$

TİYDS DÜVÜK

$$\Delta(2 \times N + 1)$$



10x

HLL

$$A = B + C;$$
$$X = Y + Z;$$

A	0
B	5
C	2
X	2
Y	1
Z	1

$$X = Y + Z;$$
$$A = B + C;$$



$$\textcircled{A} = B + C$$

$$X = \textcircled{A} \times 4$$

A	7 0 7
B	5
C	2
X	1 4 8
Y	1

$$X = A + Y$$

$$A = B + C$$

SEQUENTIAL



∞

HLL

hello.c

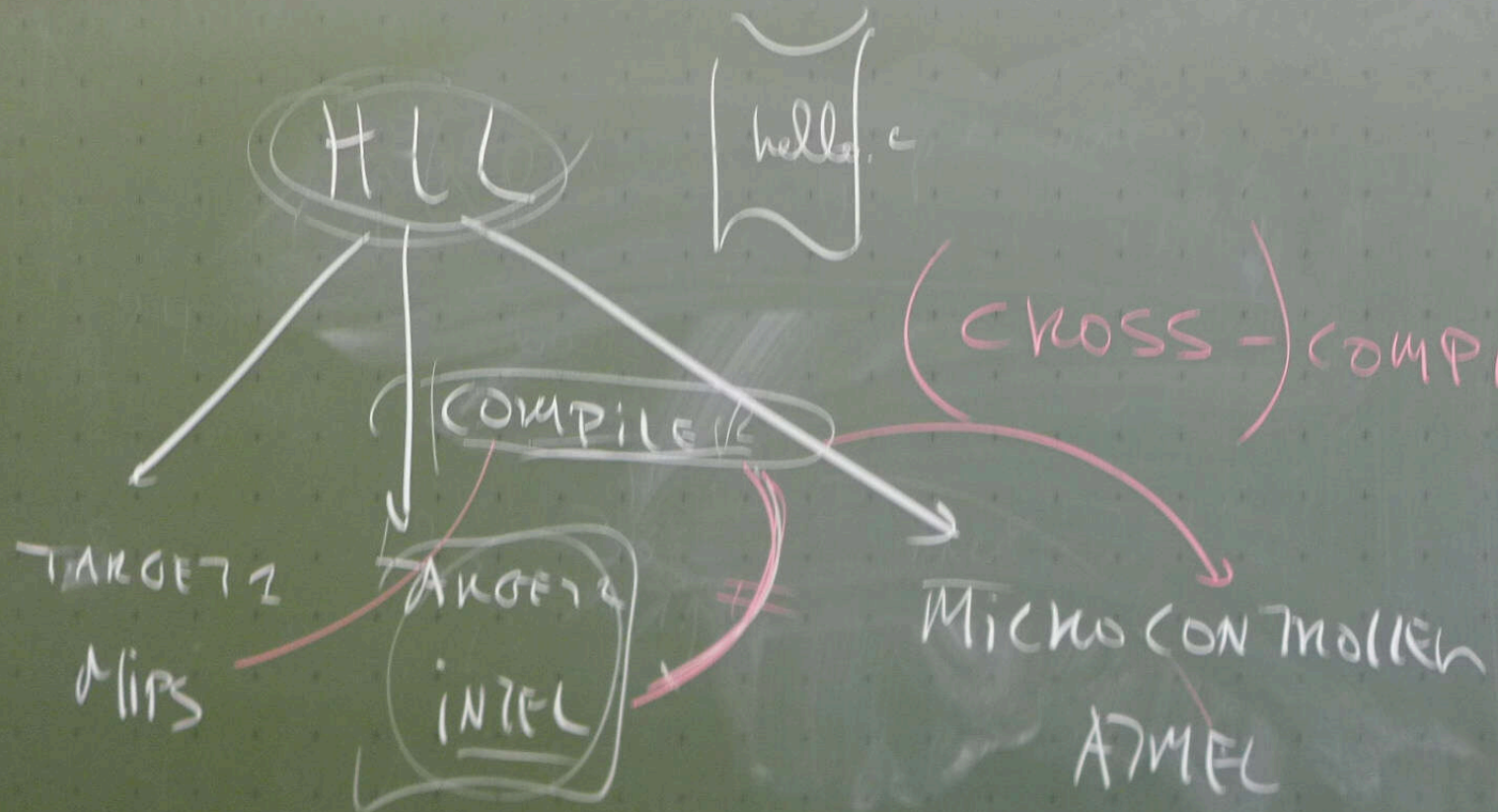
COMPILER

TARGET 1
MIPS

TARGET 2
INTEL

MICROCONTROLLER
ATMEL

(CROSS) - COMPILATION



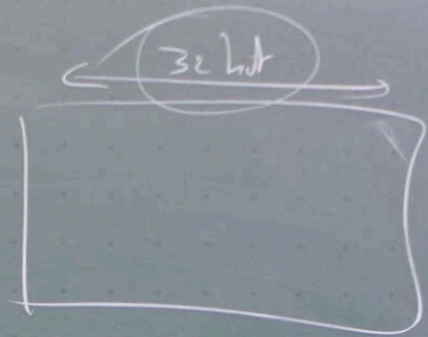
C int i;

STRONGLY TYPED
i = 10;

~~STATIC i = "ABCDEF";~~

~~i = 10 + "ABC"~~
int string

PYTHON
STRONGLY TYPED
DYNAMIC



STRING STR;

STR = "ABC";

STR = STR + "xyz";
string string

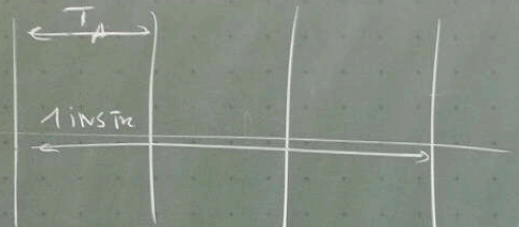
+ : string x string
→ string

$i = 10$

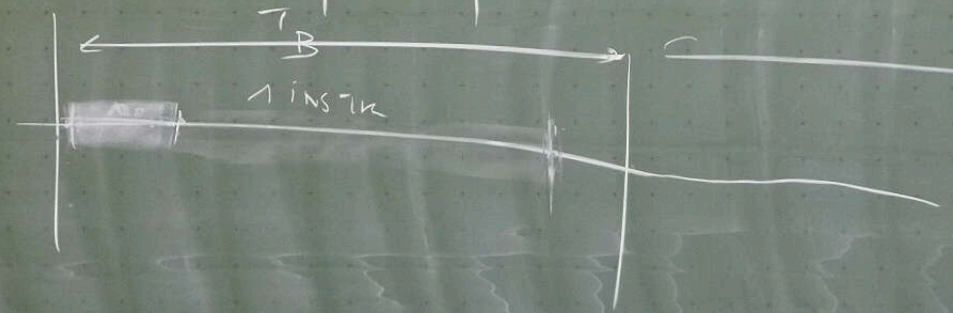
$i = \text{"ABC"}$

~~**~~ py object

PROC A
ADD



PROC B
ADD
MULT

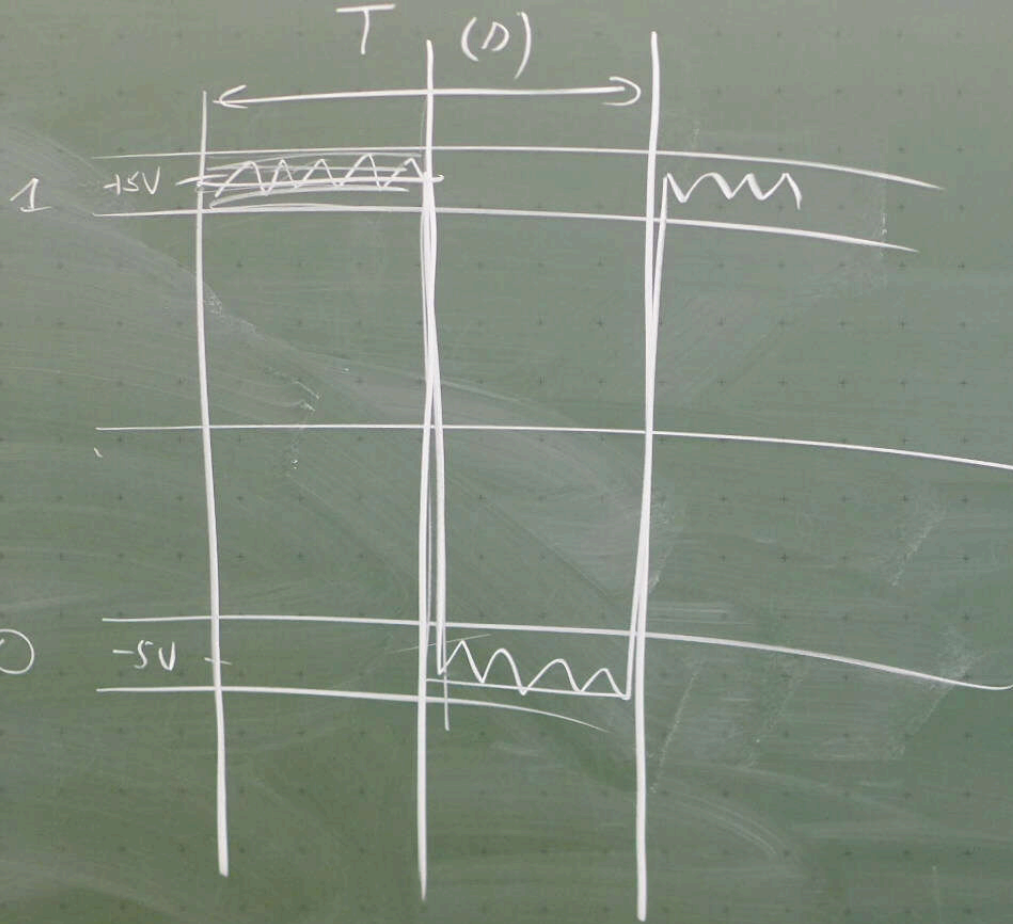


3 ADD INSTRUCTION

$3 \times T_A$

3 ADD INSTRUCTION
3 MULT INSTRUCTION

$3 \times T_B$
 $3 \times T_B$



$$\lambda = \frac{1}{\frac{1}{\lambda} = H_2}$$

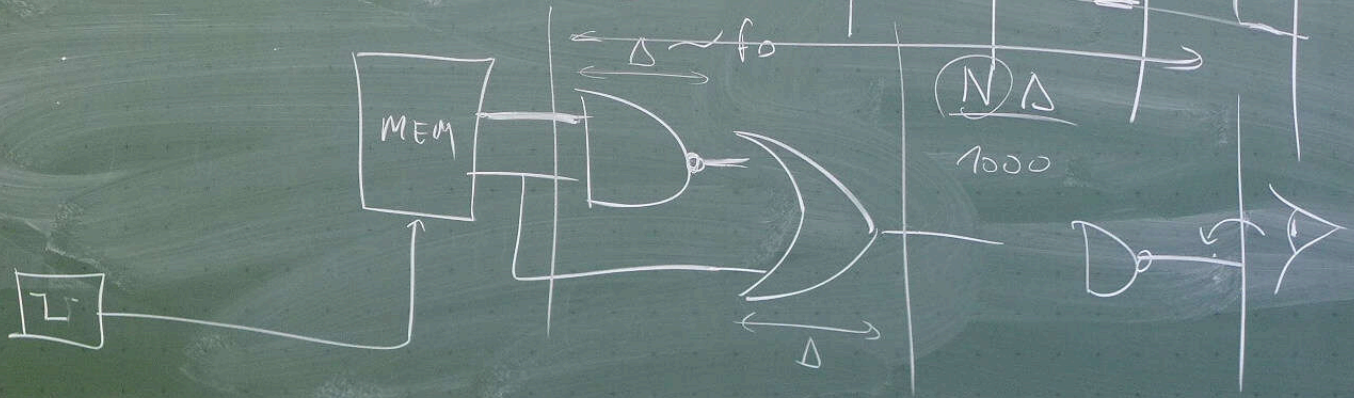
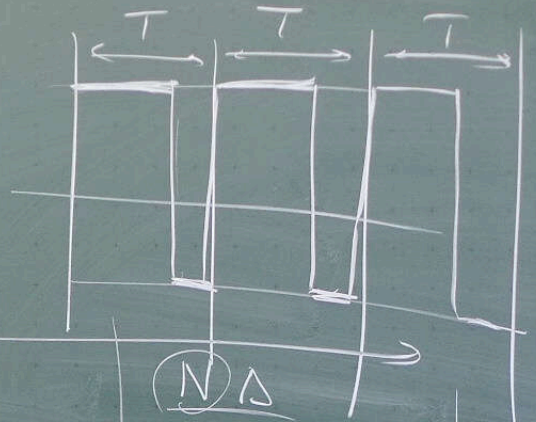
m	-3
μ	-6
h	-5
p	-12
f	-15

$$D = \frac{1}{T} \left(\frac{1}{2} = H_2 \right)$$

COMPUTE - BOUND

I/O - BOUND

- m - 3
- μ - 6
- h - 9
- p - 12
- f - 15



$$\text{CPU TIME}_A = \frac{\text{INSTN COUNT}_A}{V_A} \times \text{CPI}_A \times T_A$$

2 250 ps

$$\text{CPU TIME}_B = \frac{\text{INSTN COUNT}_B}{V_B} \times \text{CPI}_B \times T_B$$

1.2 500 ps

$$\frac{\text{CPU TIME}_A}{\text{CPU TIME}_B} = \frac{2 \times 250 \text{ ps}}{1.2 \times 500 \text{ ps}}$$

$$= \frac{1}{1.2}$$

$$10 \Delta = \text{CPU TIME}_A = \frac{\# \text{ CPU}_A \text{ CLOCK CYCLES}}{\text{CLOCK RATE CPU}_A} \Delta$$

$$6 \Delta = \text{CPU TIME}_B = \frac{\# \text{ CPU}_B \text{ CLOCK CYCLES}}{\text{CLOCK RATE CPU}_B} = 1.2 \times \frac{\# \text{ CPU}_A \text{ CLOCK CYCLES}}{\text{CLOCK RATE CPU}_B}$$

$$\frac{10}{6} = \frac{\cancel{\# \text{ cycles}_A} \times \text{CLOCK RATE CPU}_B}{2 \times 10^9 \times \cancel{\# \text{ cycles}_A} \times 1.2}$$

$$\text{CLOCK RATE CPU}_B = \frac{2 \times 10^9 \times 2 \times 10^9}{1.2} = 3.33 \times 10^9 \text{ Hz}$$

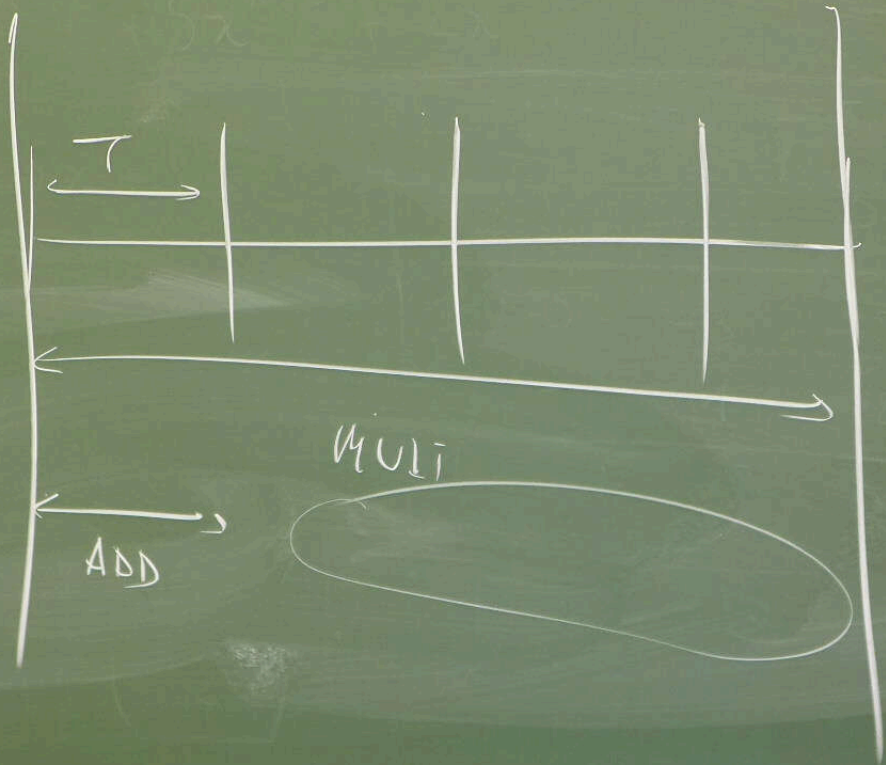
$$F = \frac{m \cdot a}{N}$$

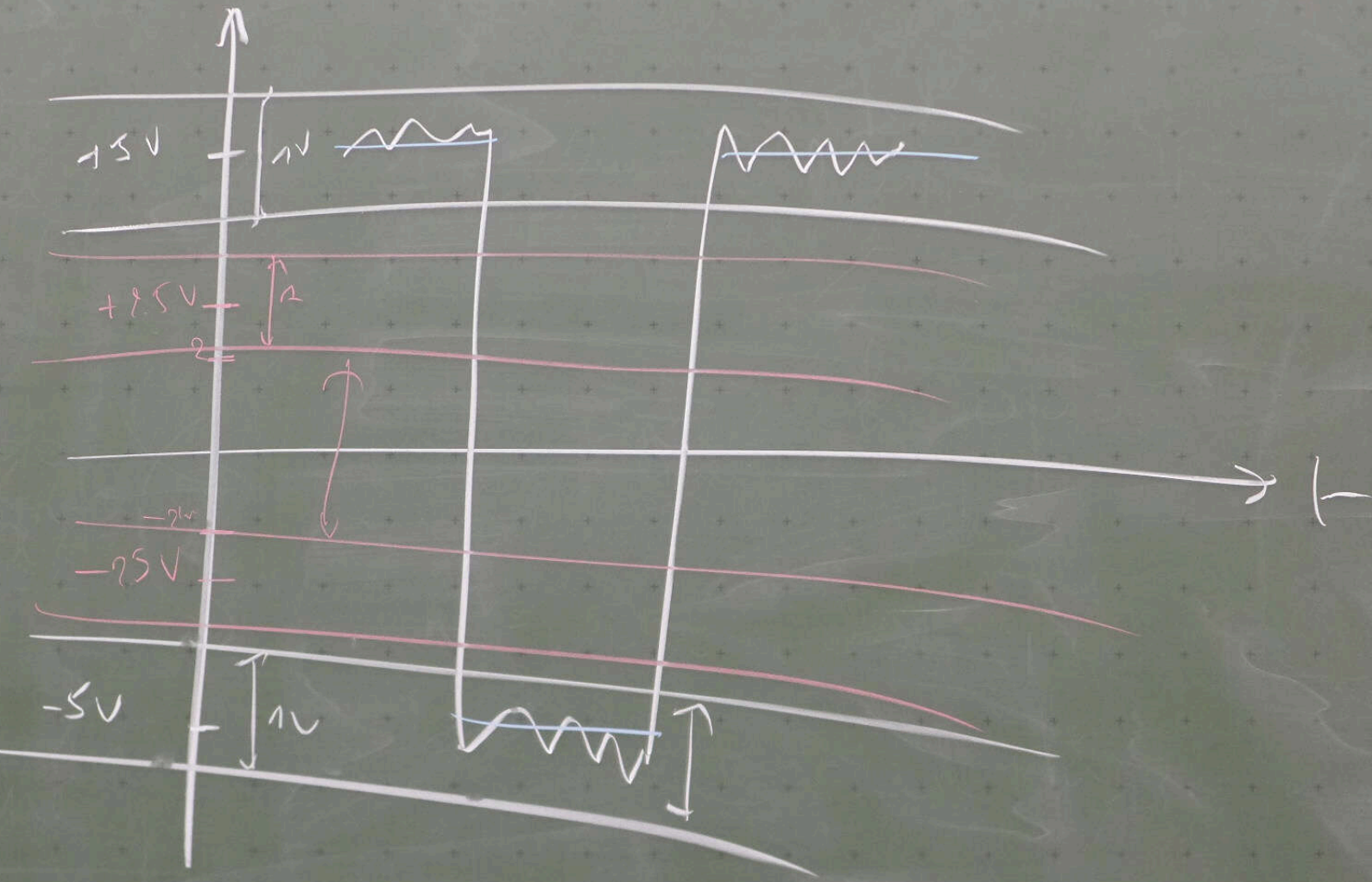
$\frac{N}{\text{kg}} \cdot \frac{\text{m}}{\text{s}^2}$

$$1.2 = 4 \times 10^9 \text{ Hz} = 4 \text{ GHz}$$

ADD — 1 clock cycles

MULT — 4 clock cycles





Peer

+10 $n+1$

ESSEN

IK

8
+10 $n+1$

+10

CSA

+4 $n+1$

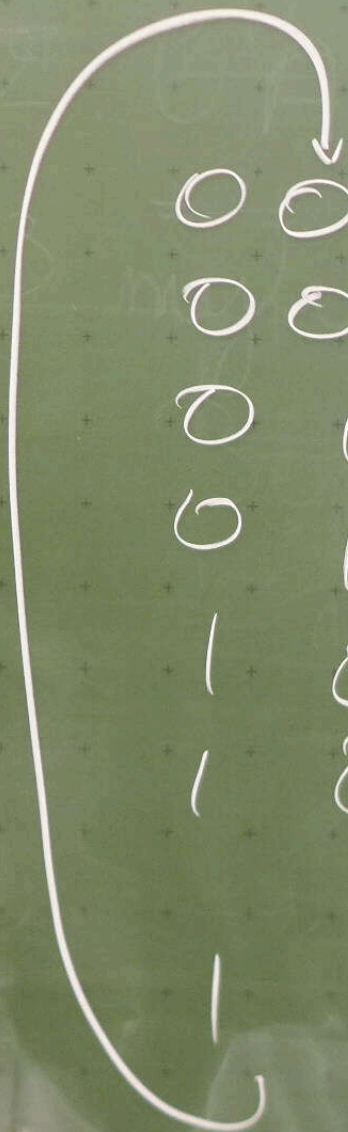
Tom

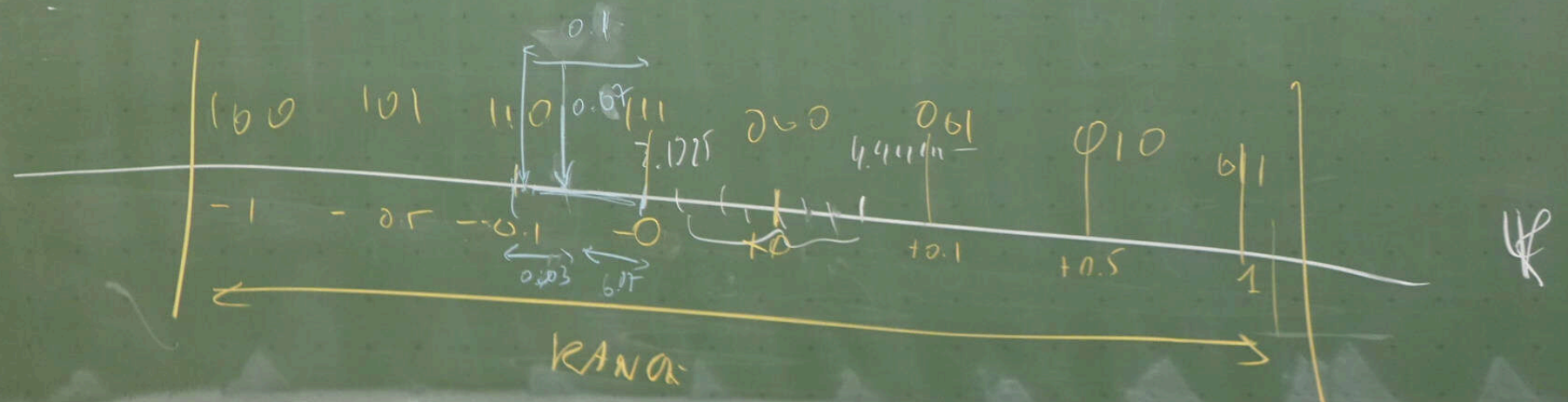
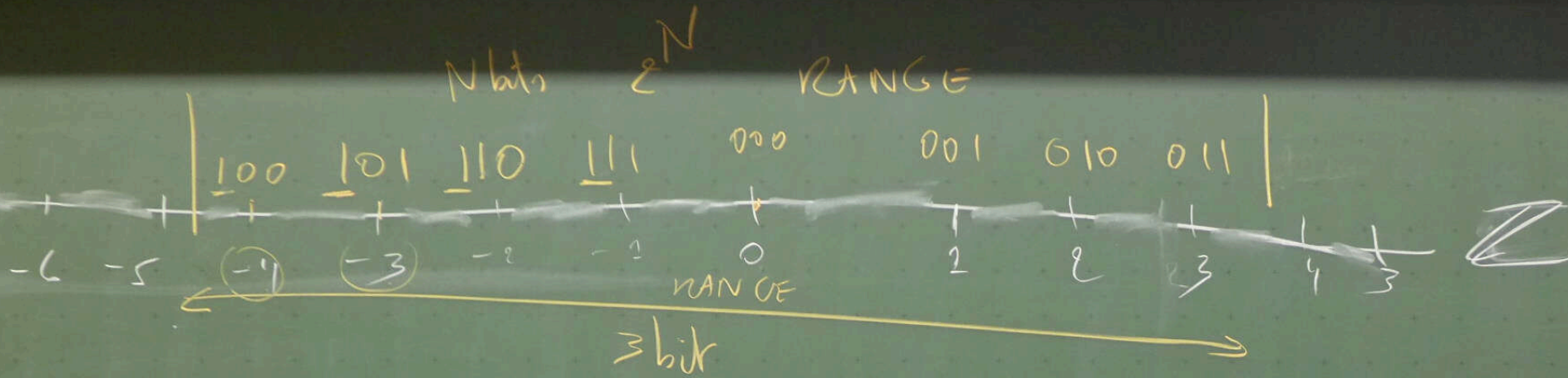
CSA

0	0	0
0	0	-
0	-	0
0	-	-
-	0	0
-	0	-
-	-	-

1	1	1	0
1	1	1	1
+	0	0	+

0	0	0
---	---	---





PRECISION?
RANGE?

$$\mathbb{N} = \{ \emptyset, 1, 2, \dots \}$$

\mathbb{X}_{\emptyset}

$$\mathbb{Z} = \{ \overset{-4}{\cancel{X}} \mid \dots -2, -1, 0, 1, 2 \dots \overset{+3}{\cancel{X}} \}$$

RANGE

$$\mathbb{Q}$$

$$\mathbb{R}$$

\mathbb{X}_{\emptyset}

\mathbb{X}_{\emptyset}

int
fixed point
float

↓ (n-1)

$$\boxed{
 \begin{array}{ccccccc}
 & n-2 & n-2 & & & & \\
 1 \times 2^{n-2} & + 1 \times 2^{n-2} & - & \dots & - & 1 \times 2^1 & + 1 \times 2^0
 \end{array}
 }$$

$$= 2 + 2 + \dots + 2 + 1$$

①

~~$$1 \times 2^n + 0 \dots = 0 \times 2^n + 0 \times 2^0$$~~

$$= 2^n + 1$$

$$2^n - 1$$

$$\left[\begin{array}{cccccccc} 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \end{array} \right]_{\text{BIN}} = 127$$

↔ 7

$$\left[\begin{array}{cccccccc} 0 & 0 & 0 & 1 & 0 & 0 & 1 & 0 & 0 & 1 & 1 & 1 \end{array} \right]_{\text{BCD}} = 127$$

↔

12	$n-2$	$n-2$	\dots	2
1×2	$+ 1 \times 2$	$+ 1 \times 2$	\dots	$+ 1 \times 2$

$$= 1 \times 2^1 + 0 \times 2^0 + 0 \times 2^{-1} + 1 \times 2^{-2}$$

$$= 2 + 0.25$$

$$= 2.25$$

10

$$\left[\text{"10.01"} \right] = 10.01$$

15₁₆

BASE 16 ENCODING

$$\left[\begin{array}{c|cc} \text{"10"} & 26 & \\ \hline 1 & -1 & -2 \end{array} \right]$$

$$\left[\text{"10"} \right] = \sum_{i=-2}^1 x_i \times 10^i$$

BASE 10 ENCODING

$$= 1 \times 10^1 + 0 \times 10^0 + 2 \times 10^{-1} + 6 \times 10^{-2}$$

$$\left[\text{"10.01"} \right] = \sum_{i=-2}^1 x_i \times 2^i$$

BASE 2 ENCODING

$$\left[\begin{array}{c|c} \text{"10.26"} & \\ \hline 1 & 4 \\ -1 & -2 \end{array} \right]$$

$$\left[\text{"10.26"} \right] = \sum_{i=-2}^1 x_i \times 10^i$$

BASE 10 ENCODING

$$= 1 \times 10^1 + 0 \times 10^0 + 2 \times 10^{-1} + 6 \times 10^{-2}$$

$$\left[\text{"10.01"} \right] = \sum_{i=-2}^1 x_i \times 2^i$$

BASE 2 ENCODING

$$= 1 \times 2^1 + 0 \times 2^0 + 0 \times 2^{-1} + 1 \times 2^{-2}$$

$$= 2 + 0.25$$

$$= 2.25$$

10

$$\left[\text{"10.01"} \right] = 10.01$$

15.16

BASE 10 ENCODING

D E A D B E E F HEX

1101 1110 1010 1011 1110 1110 1111 BINARY

1101101110
 |
 2
 2
 2
 0
 ?

MEMOIZATION

(10)

1x 3

3

2x 3

6

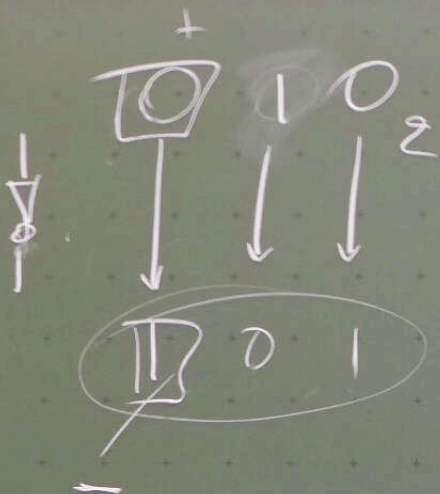
4x 3

12

5x 3

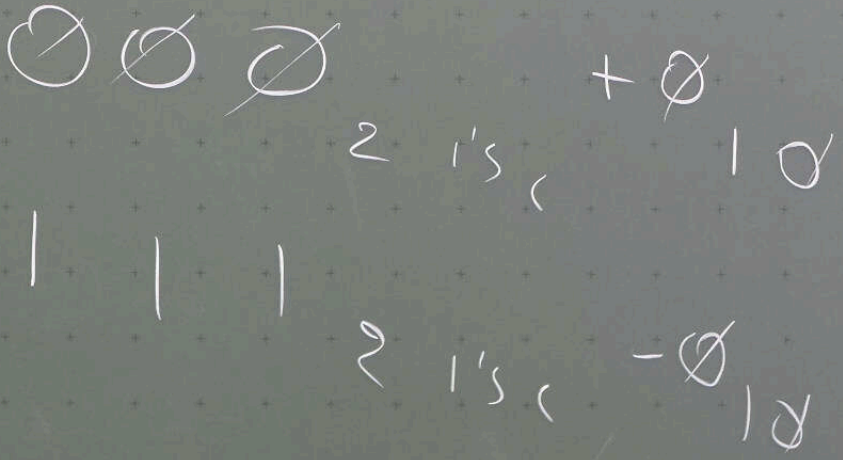
15

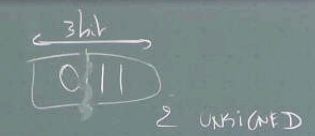
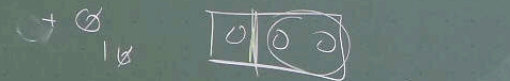
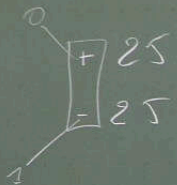
⋮



UNSIGNED 2_{10}
 SIGNED 1's comp

SIGNED -2_{10}
 1's comp





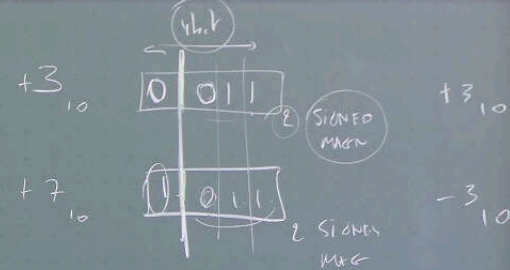
RANGE = $\left[\begin{matrix} -(2^{N-1}-1) \\ -3 \\ +3 \\ +(2^{N-1}-1) \end{matrix} \right]$

N bit

1 SIGN

N-1 VALUE

$[0, 2^{N-1}-1]$



$$A < B ?$$

$$(A - B) < \emptyset$$

$$A + \bar{B} + 1$$

$$A - B = A + (-B)$$

$$+ 3.4 \times 10^2$$
$$5.16 \times 10^3$$

$\sqrt{\quad}$?

$$\boxed{\begin{array}{l} 3.4 \times 10^2 \\ 5.16 \times 10^0 \end{array}}$$

$$55.0 \times 10^2$$

$$\boxed{111} \text{ 3-bit unsigned int} = 7$$

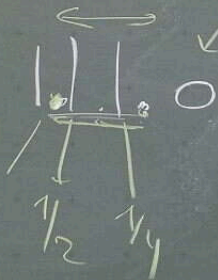
$$\boxed{111} \text{ 3-bit 2's compl int} = -1$$

$$s = 2 = 4$$

$$\boxed{111} = 7/4 \quad 10$$

UNSIGNED FIXED-POINT, 3 bit

$$\boxed{111} \text{ S=4 SIGNED} = -1/4$$



1.75

FIXED-POINT \rightarrow bits

$$S = 2^f, \text{ SIGNED}$$

2's comp \leftarrow

$$\text{RANGE} = \left[\frac{-2^{n-1}}{2^f}, \frac{2^{n-1}-1}{2^f} \right]$$

$$\text{PRECISION} = \frac{1}{2^f}$$

$$2^{(n-1)-k}$$

$$A_I \begin{bmatrix} 0 & 1 & 1 & 0 & 1 \end{bmatrix} = \text{O}$$

$$B_I \begin{bmatrix} 0 & 1 & 1 & 1 \end{bmatrix} = S$$

$$A_I \cdot B_I \begin{bmatrix} \\ \\ \\ \\ \end{bmatrix} = M$$

$$\left| \pi - 3.15625 \right| < \frac{1}{25}$$

6

$$\left[\begin{array}{c} 0 \\ b^{\frac{n-1}{2}} \end{array} \right]$$

$$\left[\begin{array}{c} -b^{\frac{n-1}{2}} \\ b^{\frac{n-1}{2}} \end{array} \right]$$

$$\left[0 / b^{\#}, b^{\#} - 1 / b^{\#} \right]$$

UNSIGNED

RANGE

$$\left[-b^{\#n-1} / b^{\#}, b^{\#n-1} - 1 / b^{\#} \right]$$

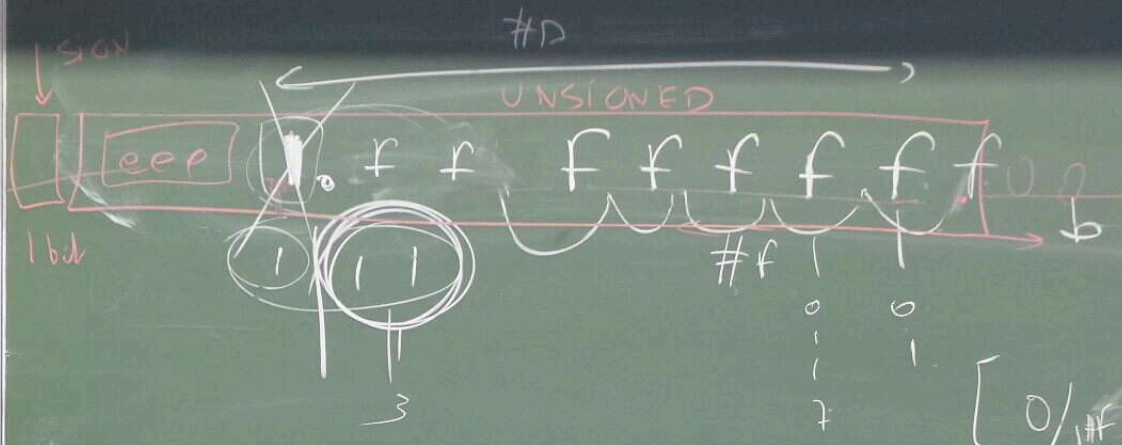
SIGNED

$$1 / b^{\#}$$

MAX ERROR

$$123000 = 123 \times 10^3$$

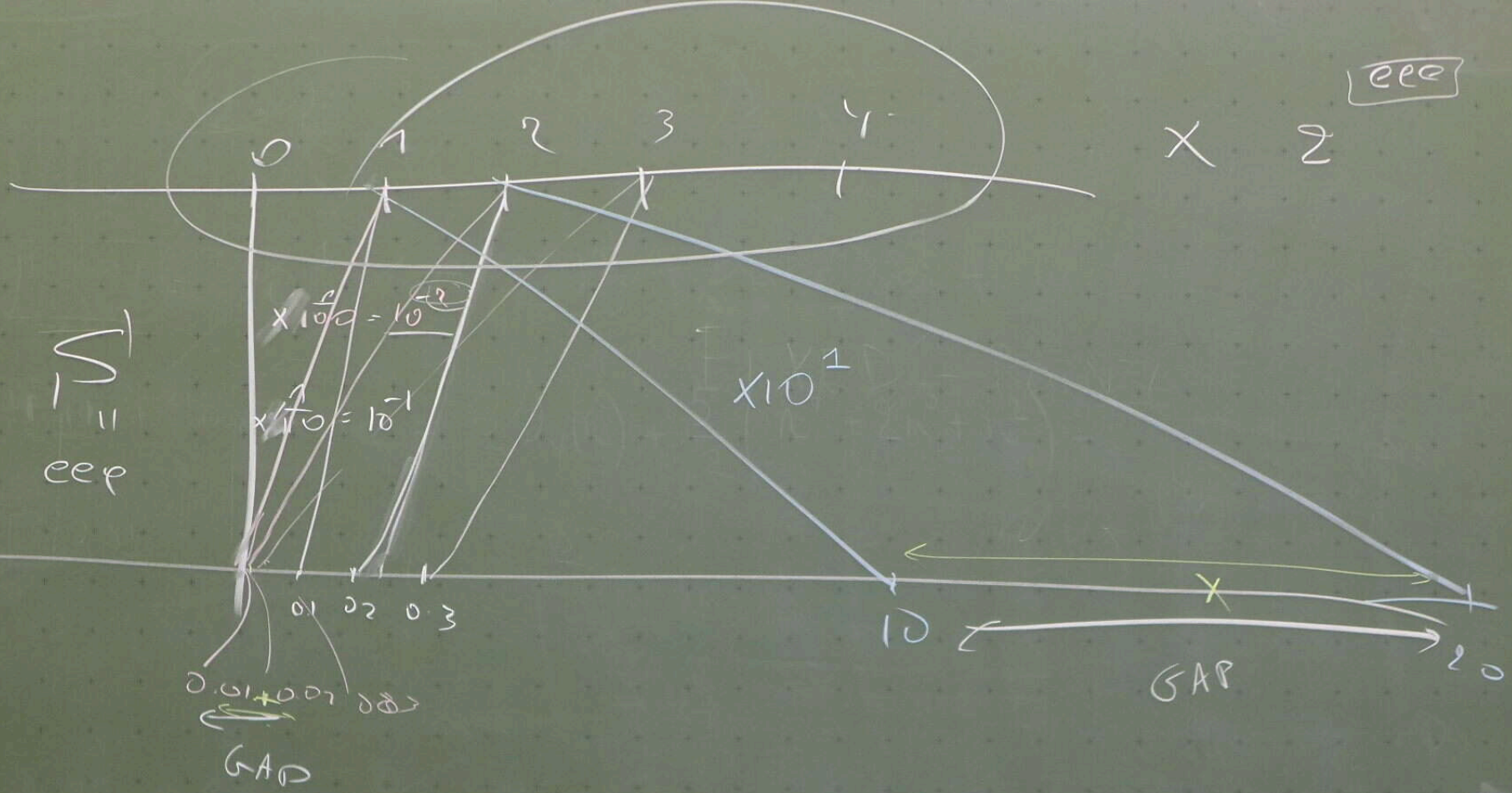
$$0.123 = 123 \times 10^{-3}$$



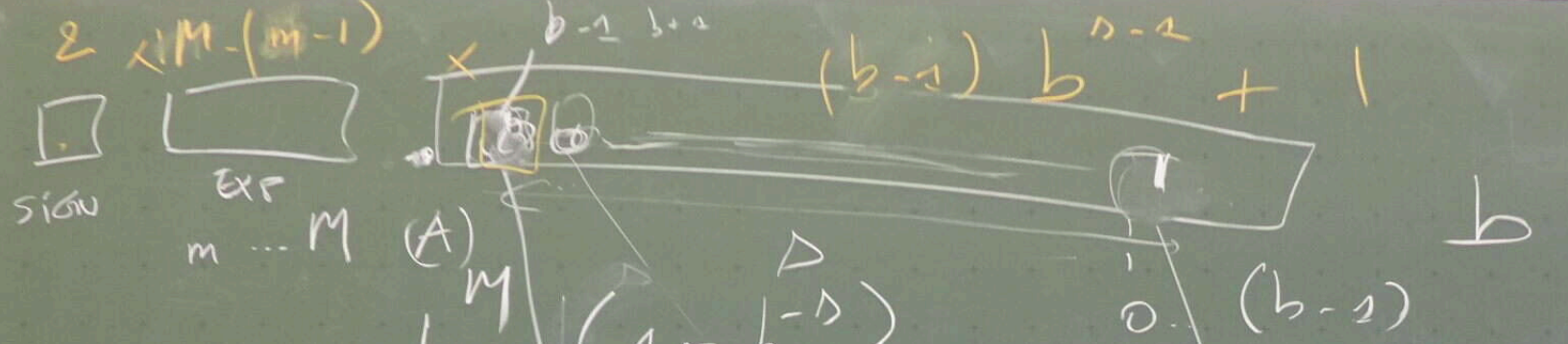
$$\#i \quad \#f = \#i + \#f$$

FIXING-POINT

[0 / b^{#i}]
[- b^{#f}]



\int_{eee}

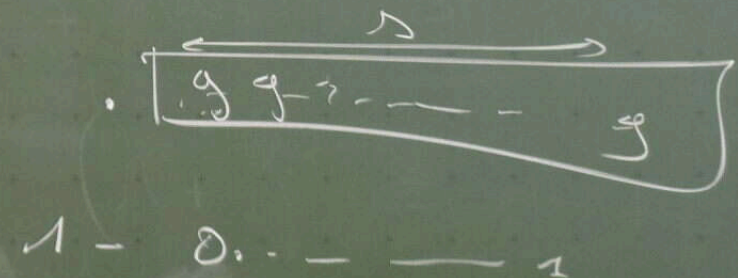


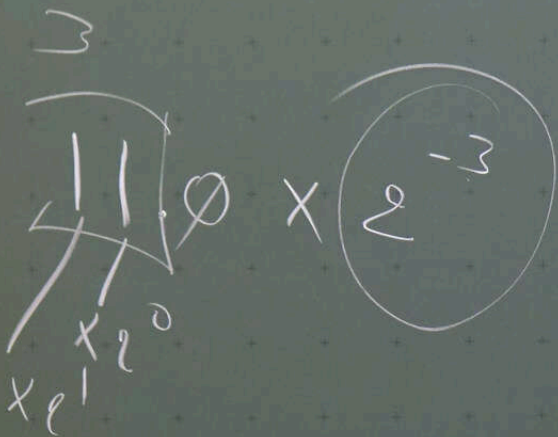
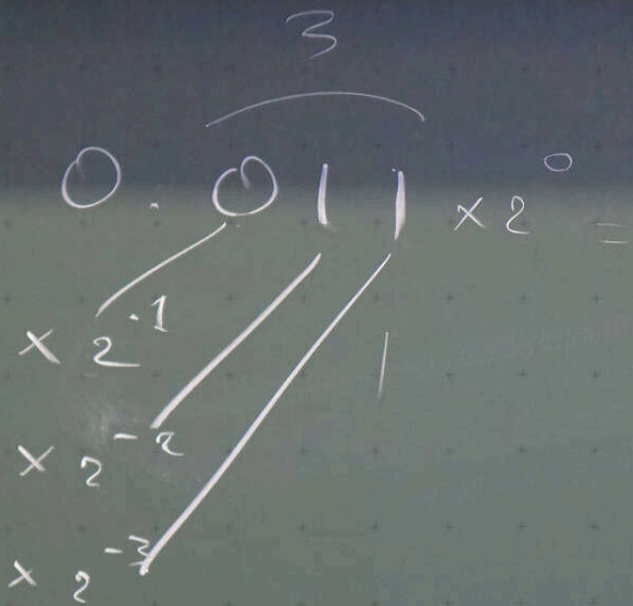
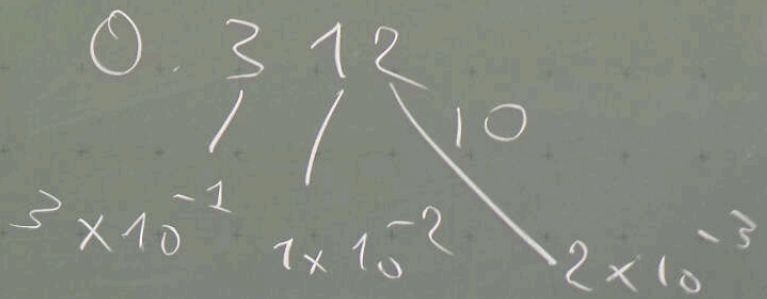
LARGEST: $+ b^m (1 - b^{-D})$

SMALLEST: $+ b^m v \times b^{-1}$

LARGEST GAP: $+ b^m \times 1 \times b^{-D}$

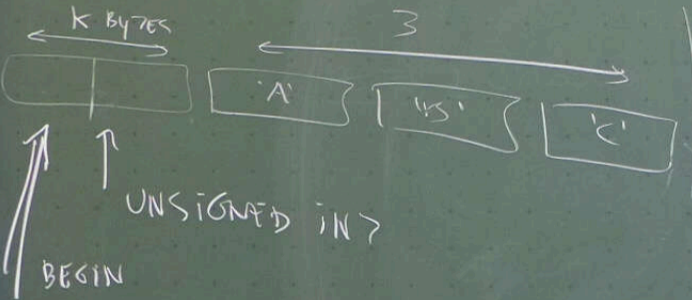
SMALLEST GAP: $b^m \times 1 \times b^{-D}$





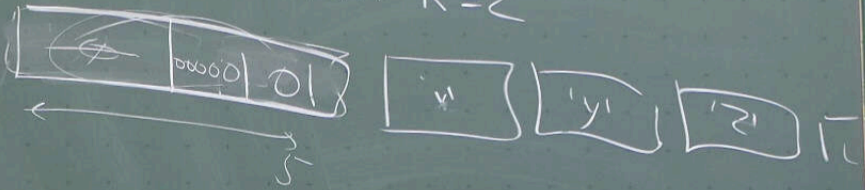
Java - STYLE

"ABC"



MEM. SPACE? 2 bytes
 TIME? $N+2$ bytes
 $O(1)$
 CONCAT $O(L_1 + L_2)$
 MAX LENGTH $2^{8k} - 1$
 JAVA

$K \text{ BYTES} = k \times 8 \text{ bits}$
 JAVA: $k=2$



$1024 \times 64 - 1$

on

AT

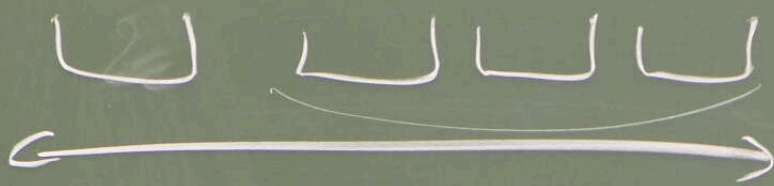
AT

SIANS SENIK

SENİK

UTF-8

UTF-8



CHAR

CHAR



2



€

"2€"

C STYLE +1

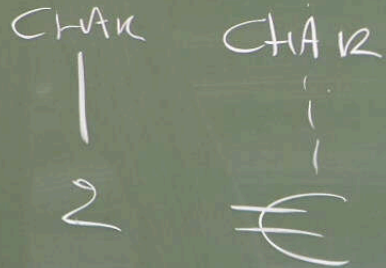
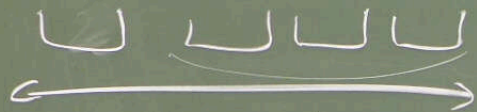
uuuuu (u)

JAVA STYLE +2

uuuuu

bytes
char ?

UTF-8 UTF-8



"2€"

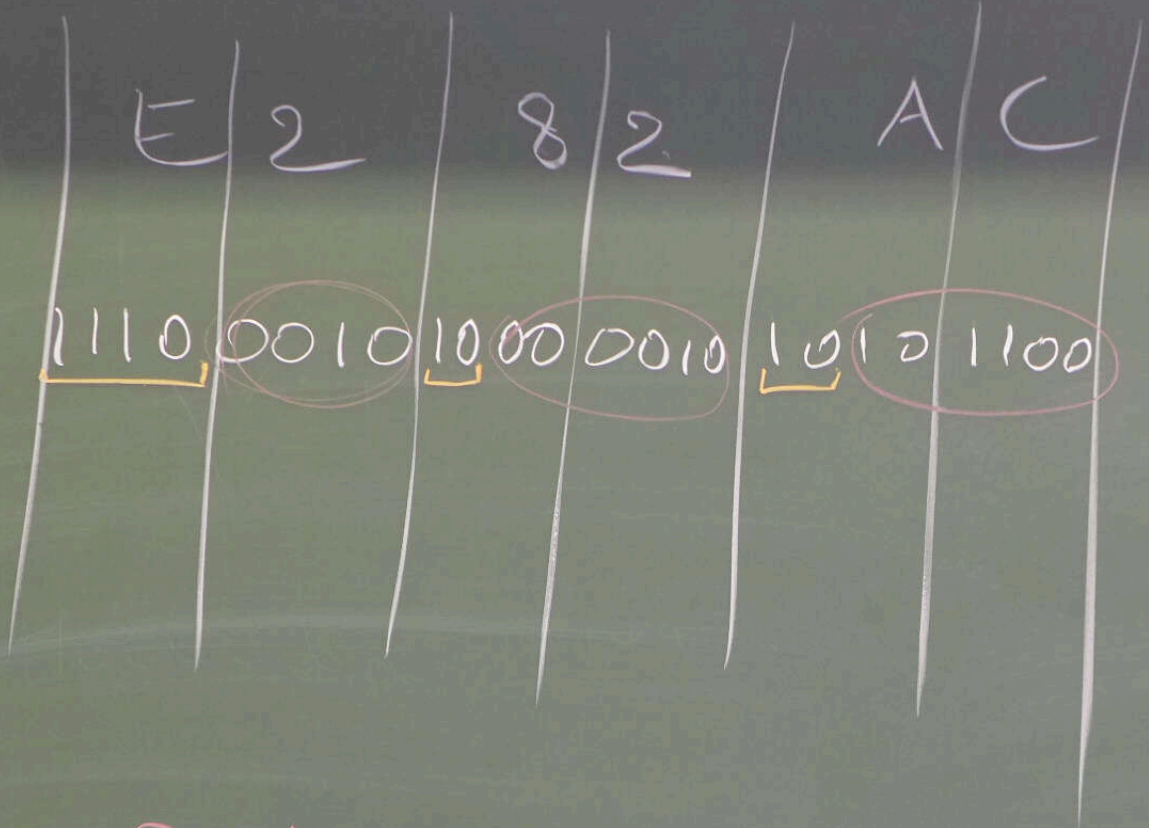
C STYLE +1



JAVA STYLE +2

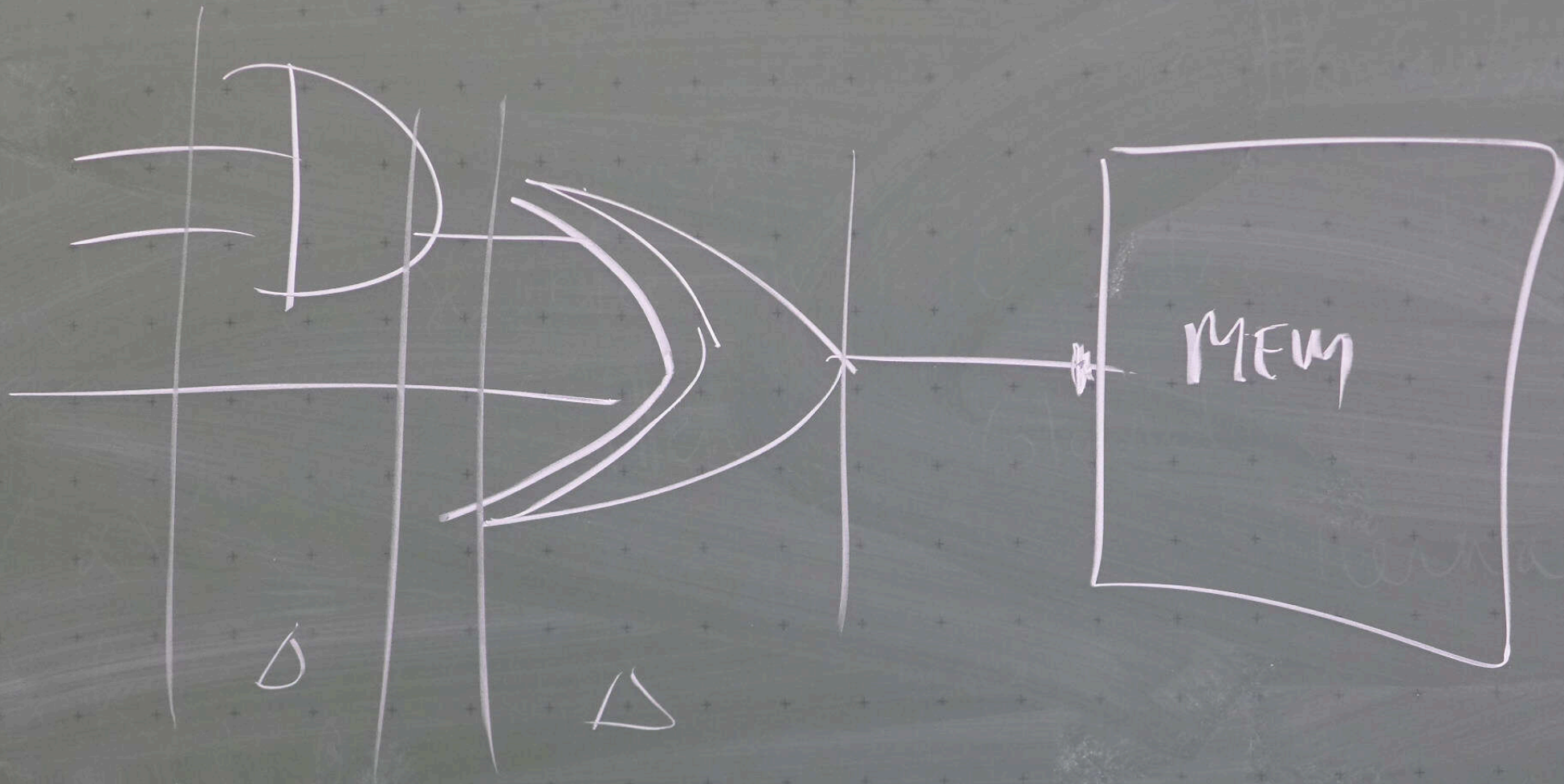


bytes
CHAR ?

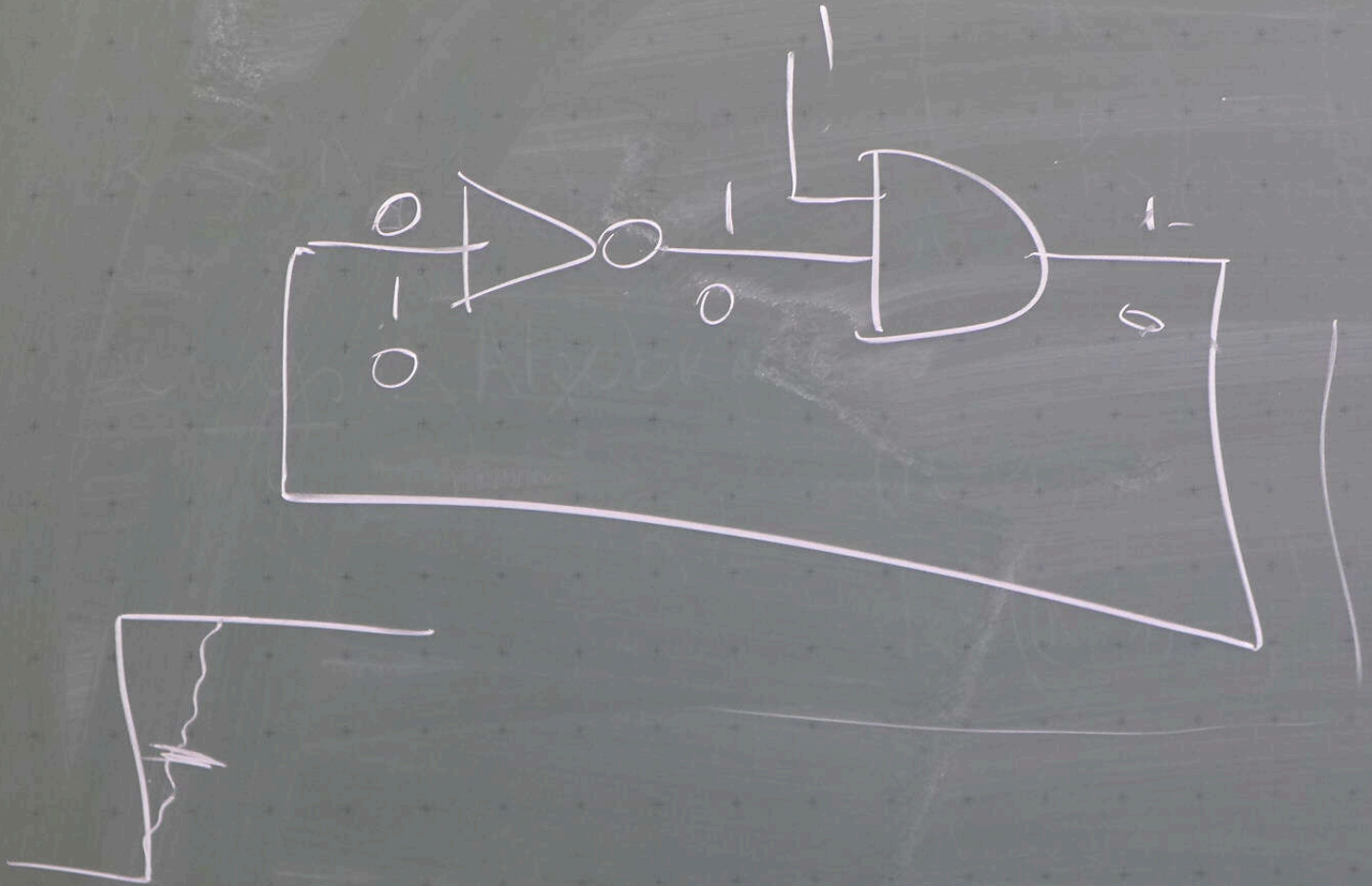


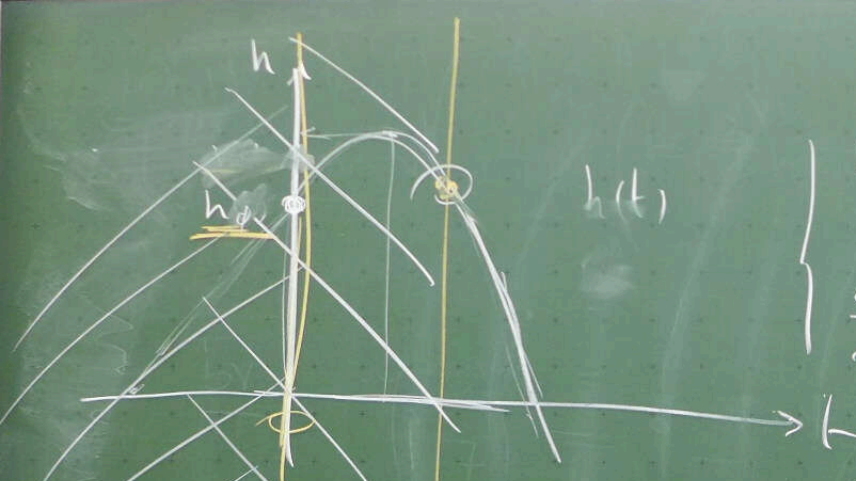
0010 00 0010 101100





META-STABLE





$h(t)$

$$\left\{ \begin{array}{l} m \frac{dv_i}{dt} = -mg \\ \frac{dh}{dt} = v \end{array} \right.$$

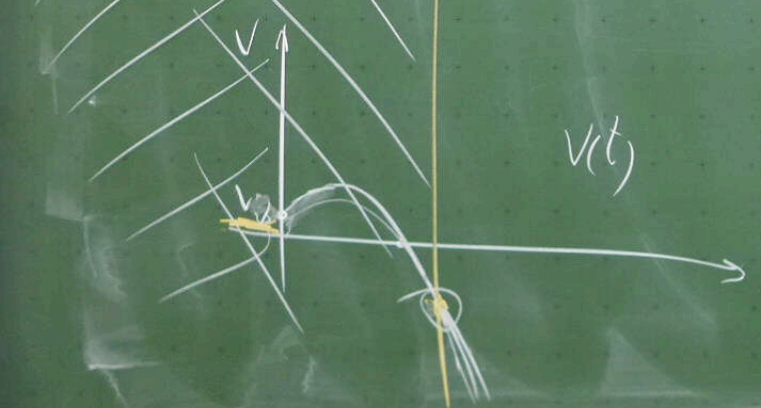
$v(0) = v_0$

"STATE"
TOESTAND
STAAT

height

$h, v : \mathbb{R} \rightarrow \mathbb{R}$

~~$\frac{dv}{dt} = a$~~



$v(t)$

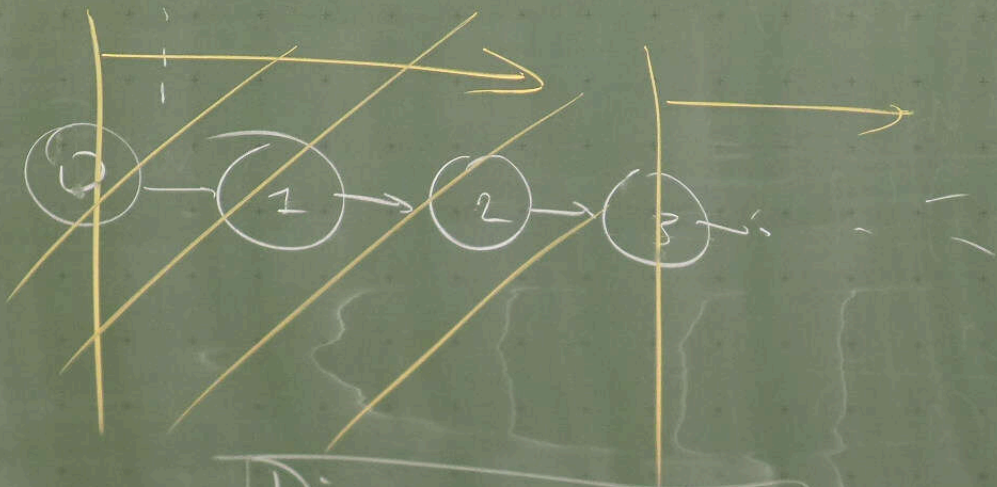
CONTINUOUS

$$\begin{cases} \underline{x(i+1)} = x(i) + 1, & i \in \mathbb{N} \\ \underline{x(0)} = x_\phi = \phi \end{cases}$$

$$x(1) = 1$$

$$x(2) = 2$$

$$x: \mathbb{N} \longrightarrow \mathbb{N}$$

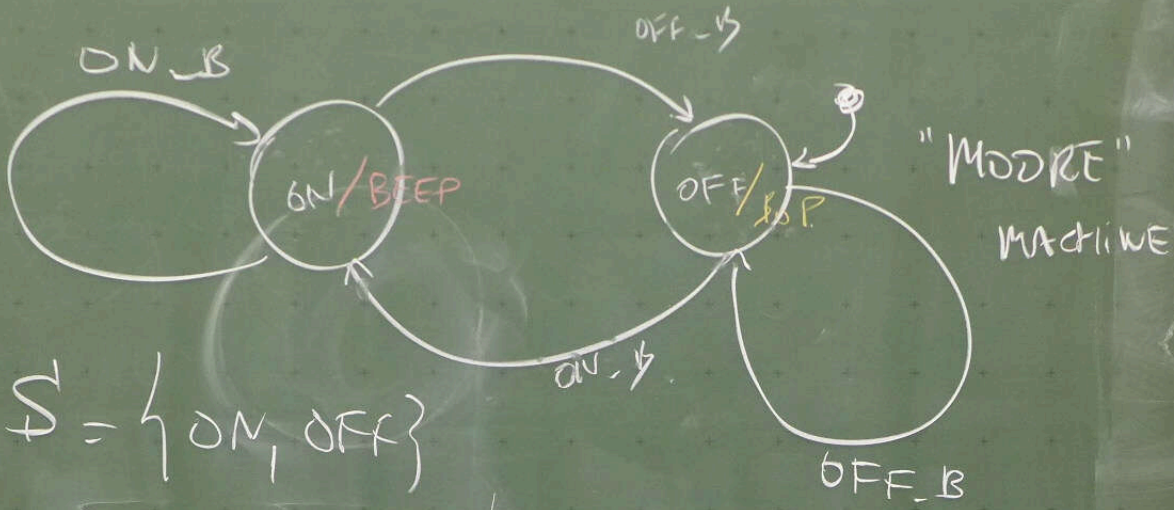


DISCRETE ∞

FSA

DISCRETE

FINITE STATE AUTOMATA



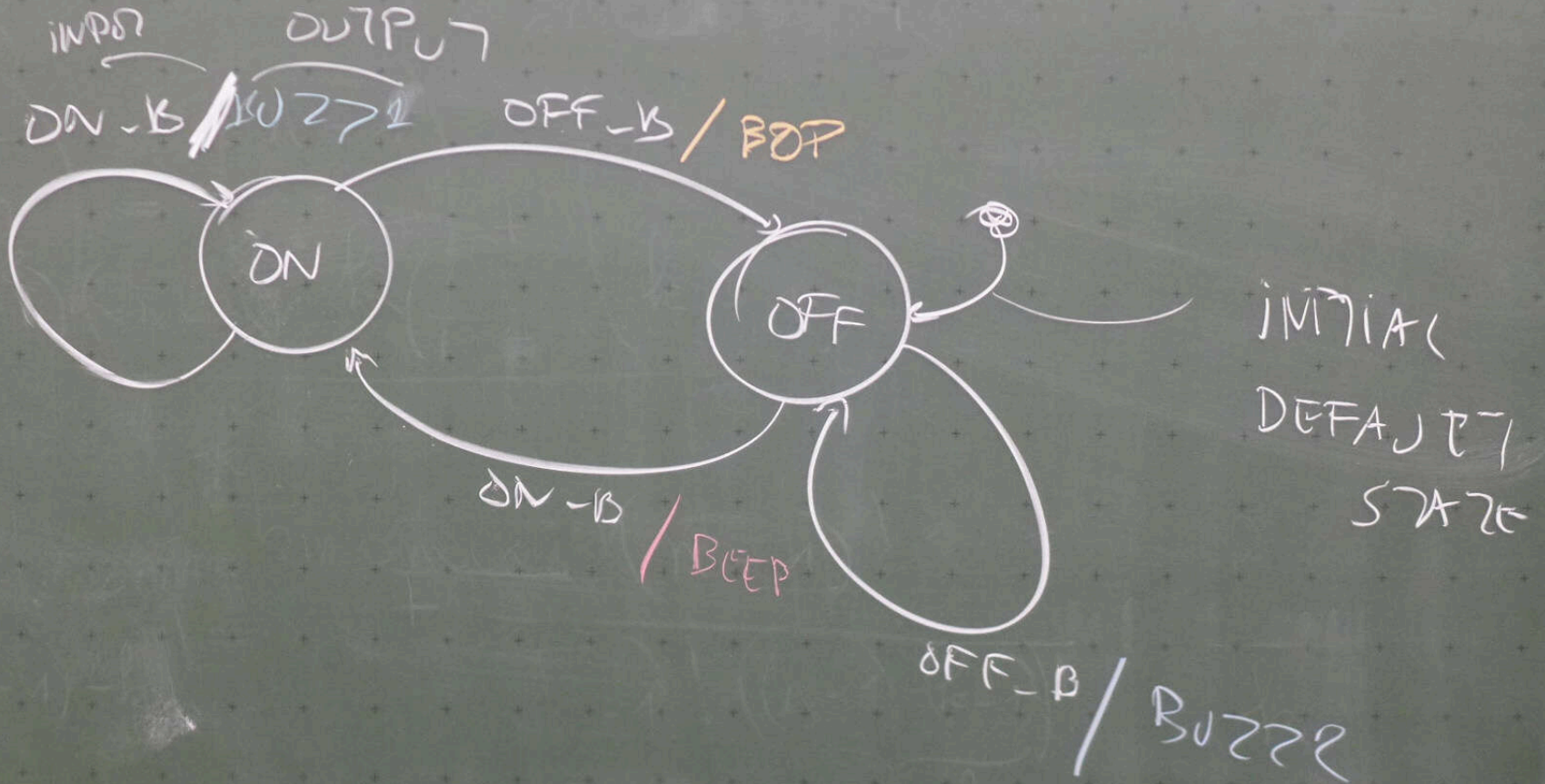
$$S = \{ON, OFF\}$$

INPUT	ON_B	OFF_B
ON	ON/BEEP	OFF/BOP
OFF	ON/BEEP	OFF/BOP

OFF

INIT

"MEALY" MACHINE



INPUT S	ON_B	OFF_B
ON	ON / BUZZ1	OFF / BOP
OFF	ON / BEEP	OFF / BUZZ2

1 1 0 1 1 0 0 0

PARITY
Bi ?

EVEN

→ DETECT

— 1 Bi ? ERROR



Δt

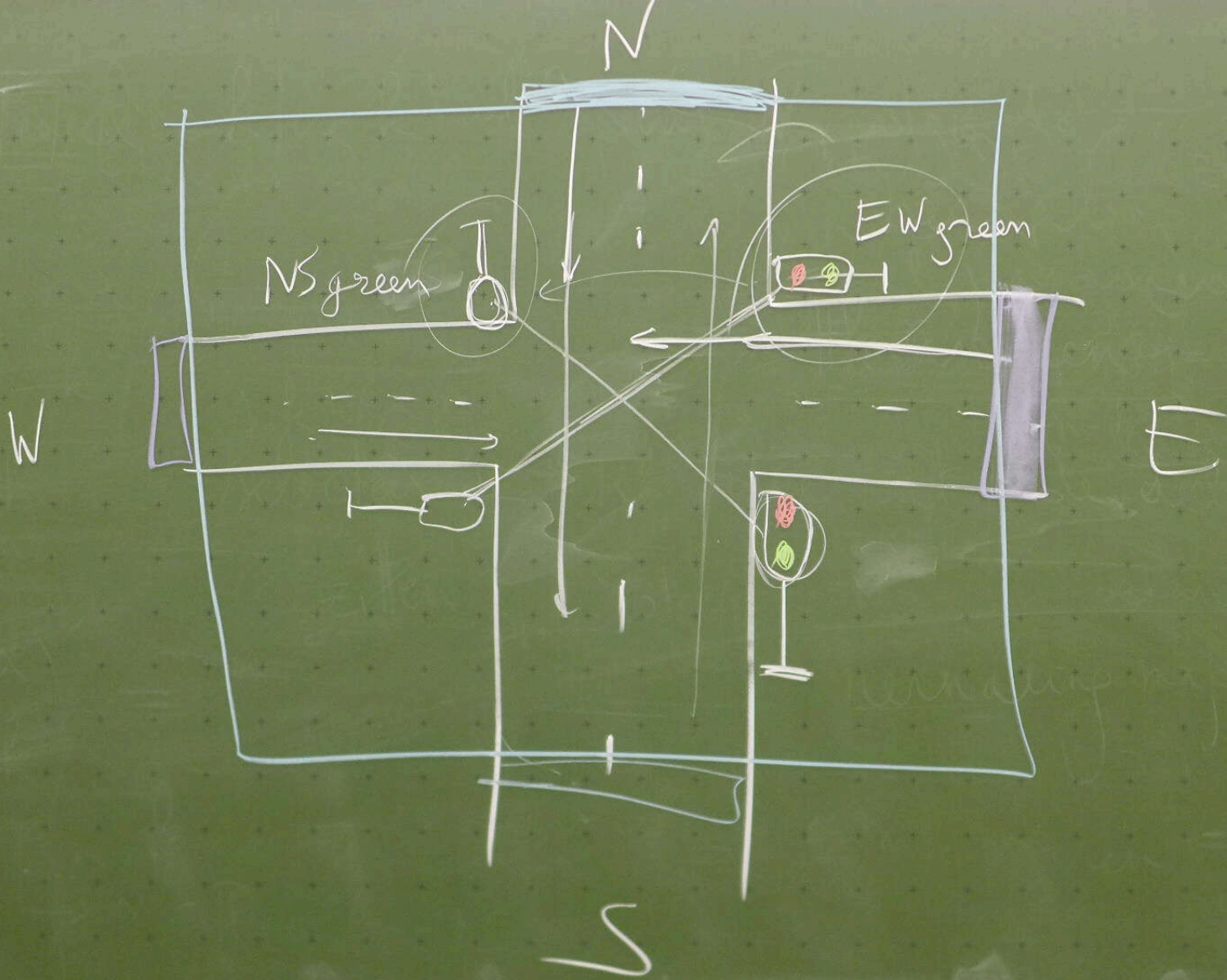
1 1 1 1 0 0 0



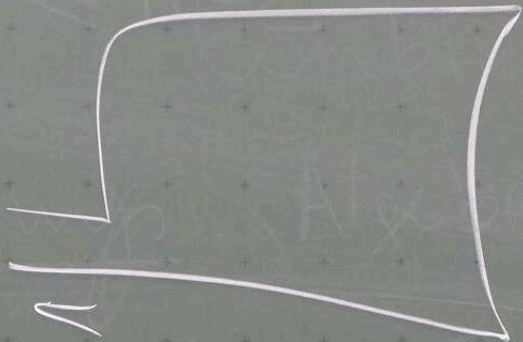
NACH



VORHER

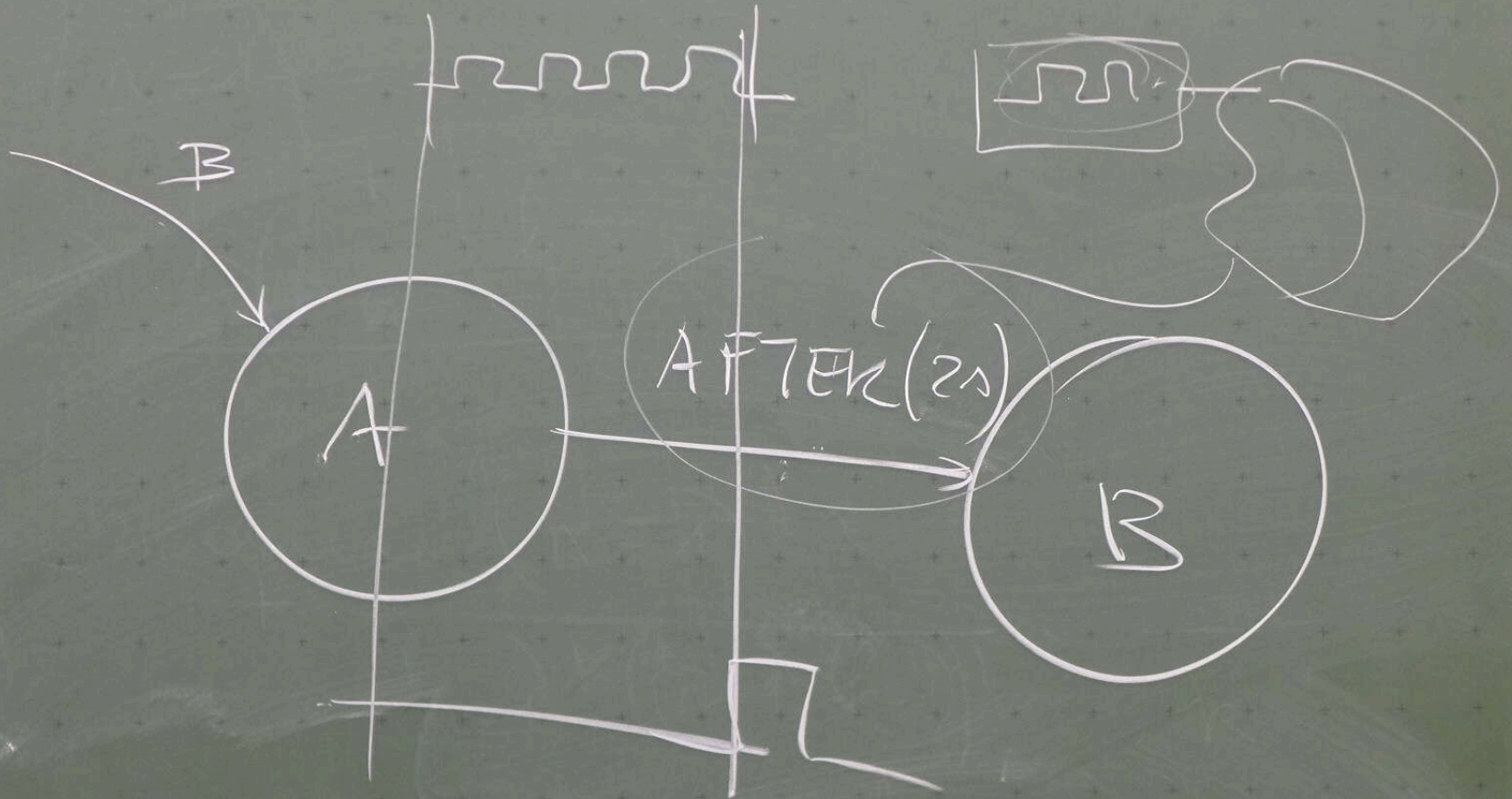


I. INDUCTION LOOP



II. PIEZO-ELECTRIC

TIMED AUTOMATA



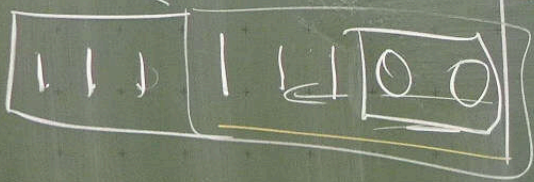
32 bit



UNSIGNED

7

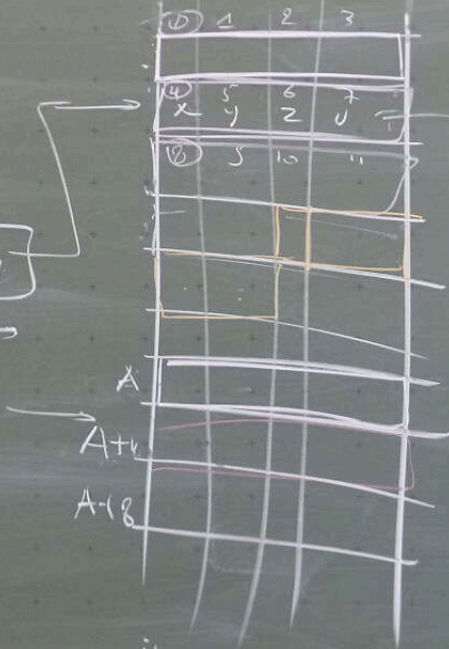
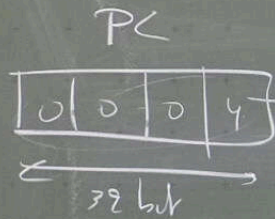
SIGN EXTEND 5 bit X4



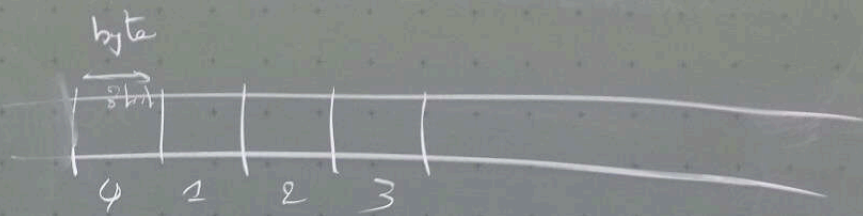
SIGNED (2's COMPL.)

-1

← 8 bit →



INSTRUCTION MEM



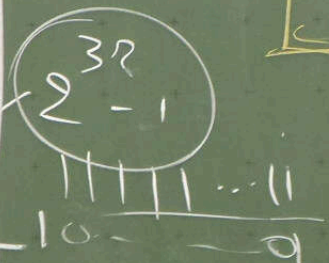
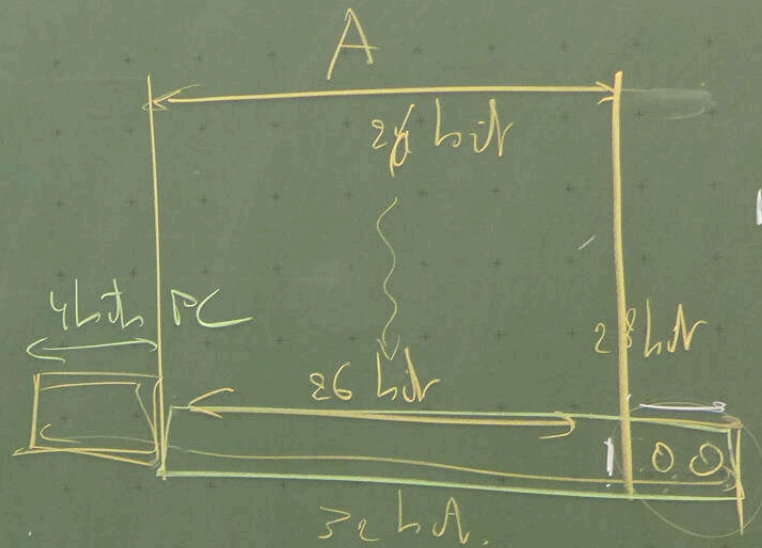
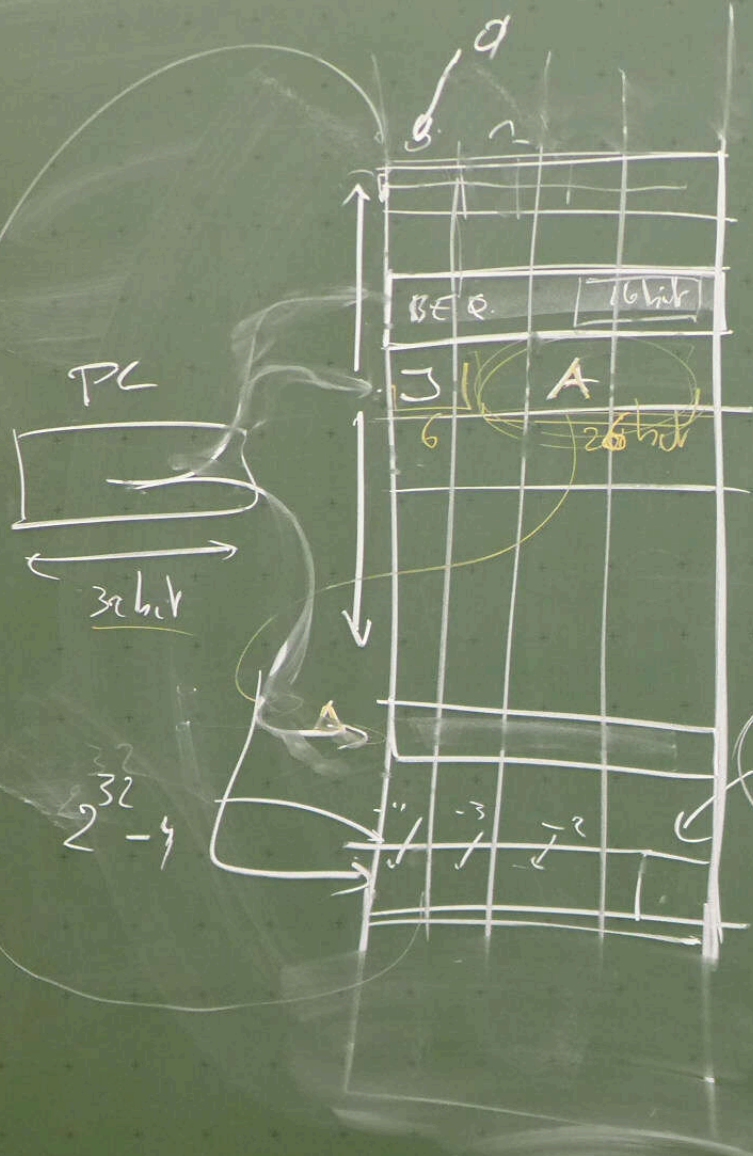
~~XYDQW~~
INSTN

PC + 4 + OFFSET

32 bit

16 bit SIGNED

INSTN MEM

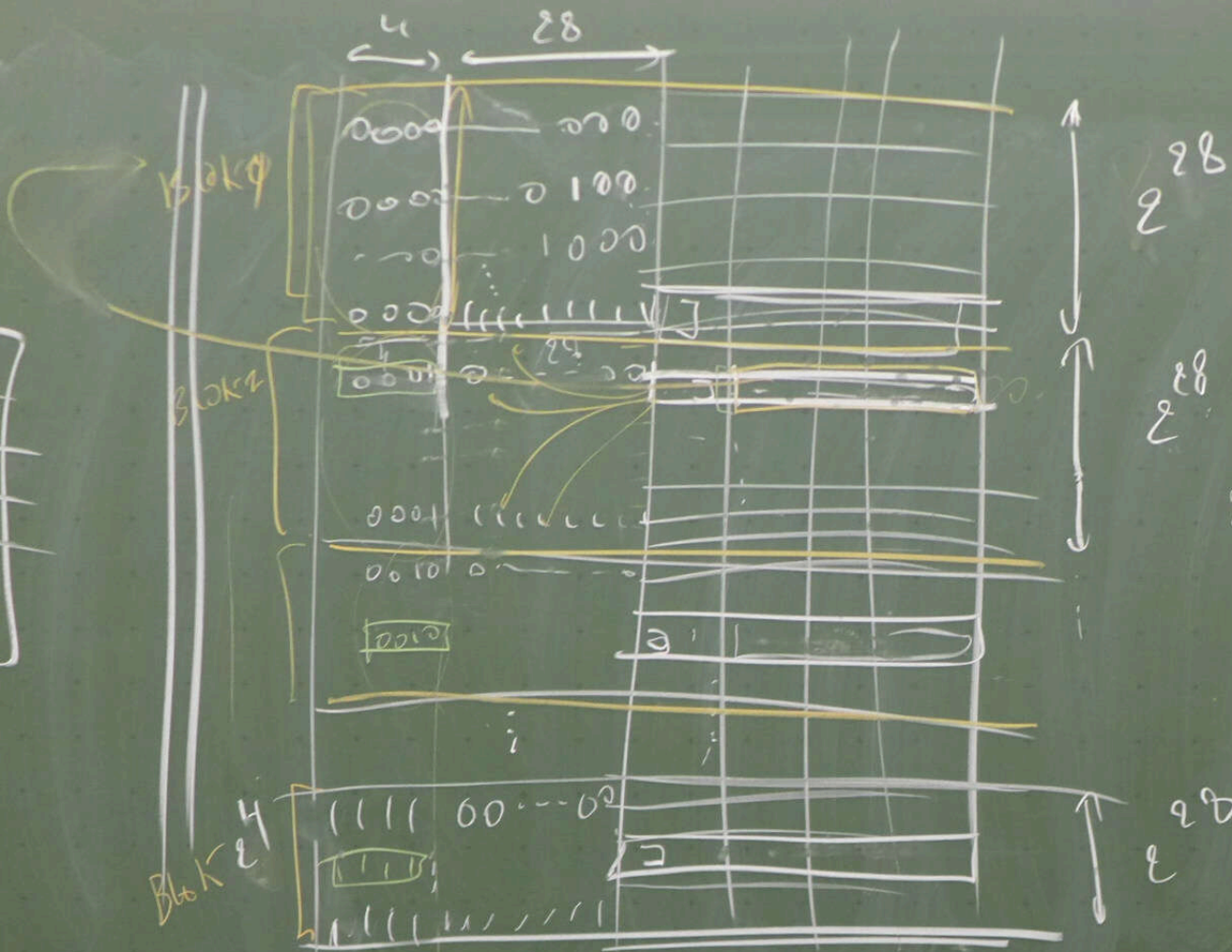


$$2^{10}$$

$$2^{30}$$

$$= 1024$$

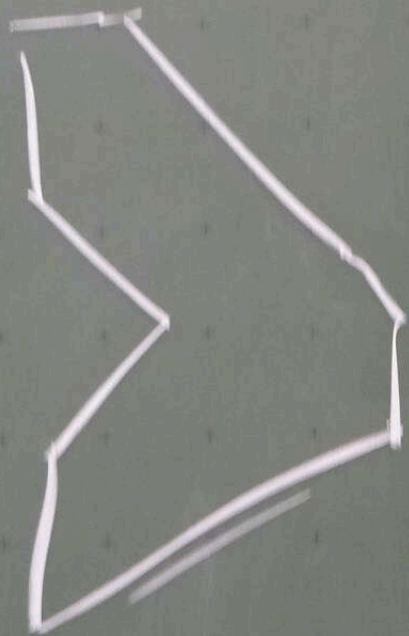
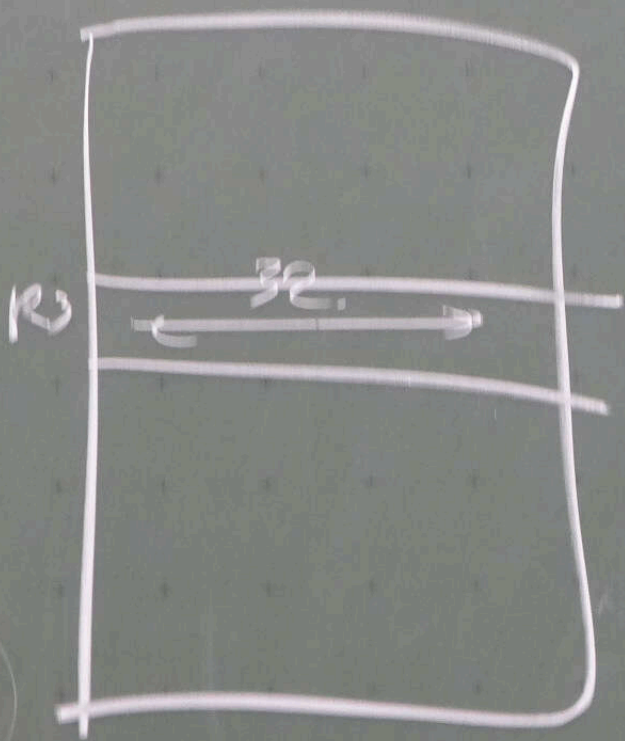
$$= 4 \times 1024 \times 1024 \times 1024$$



$$2^4 \times 2^{28} = (2^{32})$$

64 M



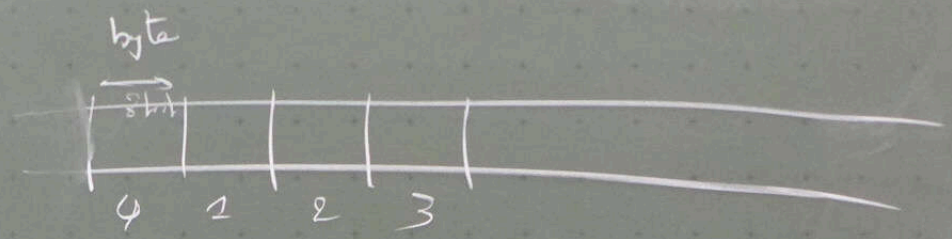
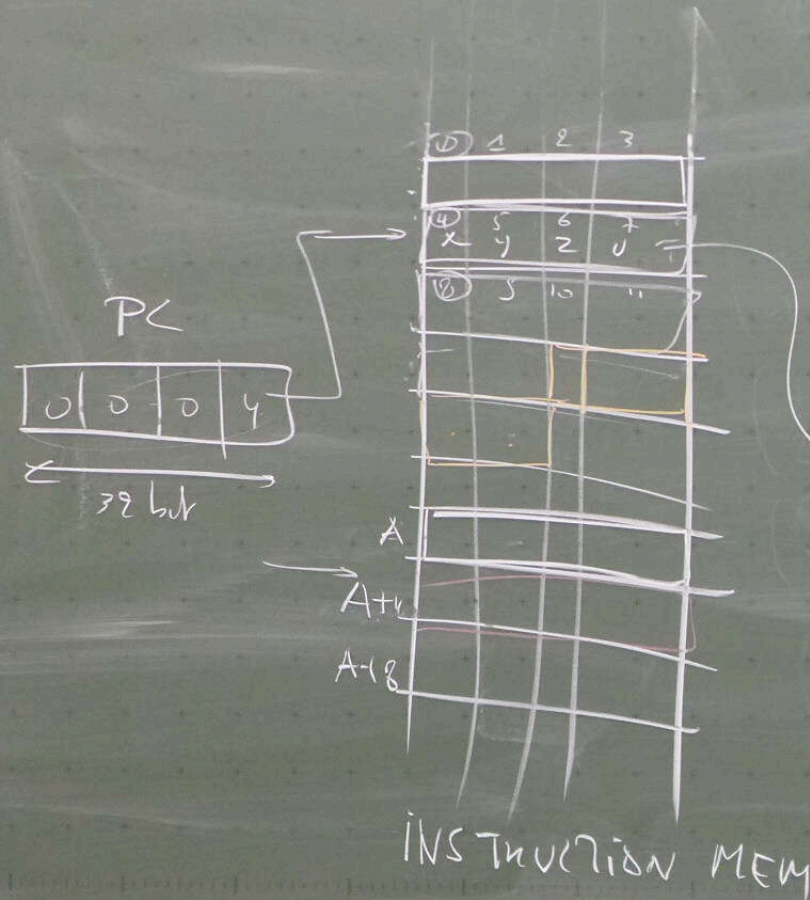


(U R 13)

DATA

MEM

10



X1Y1010101
INSTR

PC + 4 + OFFSET

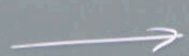
32 bit

16 bit SIGNATURE

INCREMENTAL



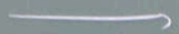
R1



TEST 1



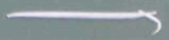
R2



TEST 2



R3



TEST 3



R4

REGRESSION TESTING

ORTHOGONAL

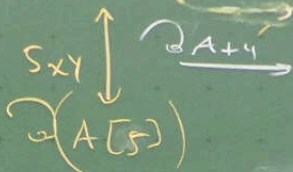
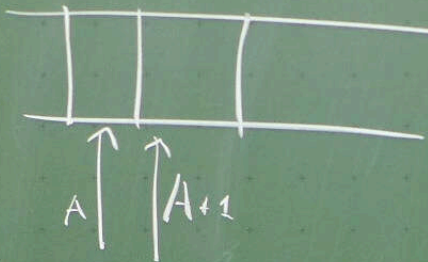
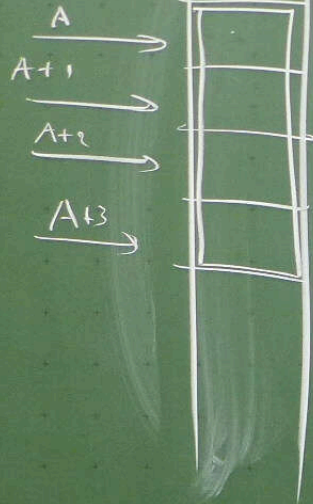
	ADD	OR	AND
3 REG	ADD	OR	AND
imm	ADD _D	OR _D	AND _D

~ HW

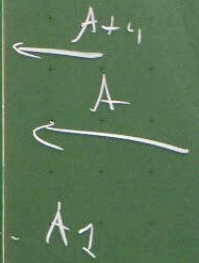
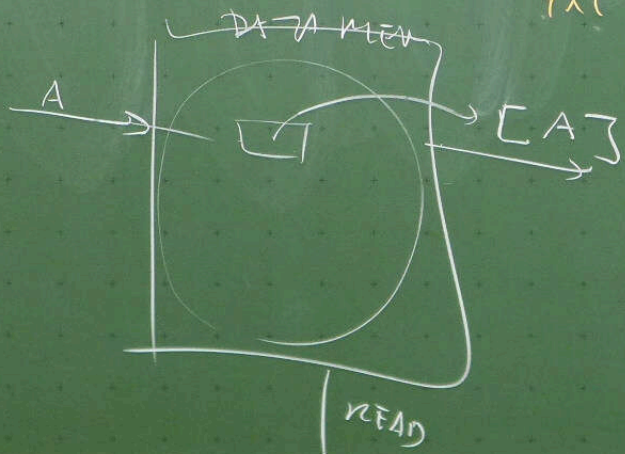
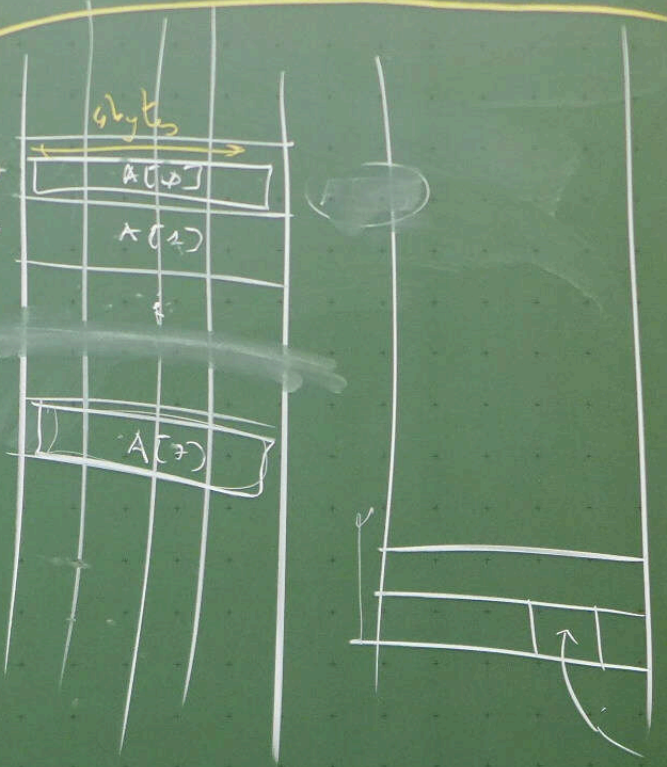
INSTRUCTION SET

8 bits
1 byte

DATA MEM



$$\text{Address}(A[i]) = \text{Address}(A[0]) + 4 \times i$$



ARRAY A OF T

$$\text{LEN}(T) = L$$

BASE ADDRESS (A) =

$$\text{OA} = \text{OA}[0]$$

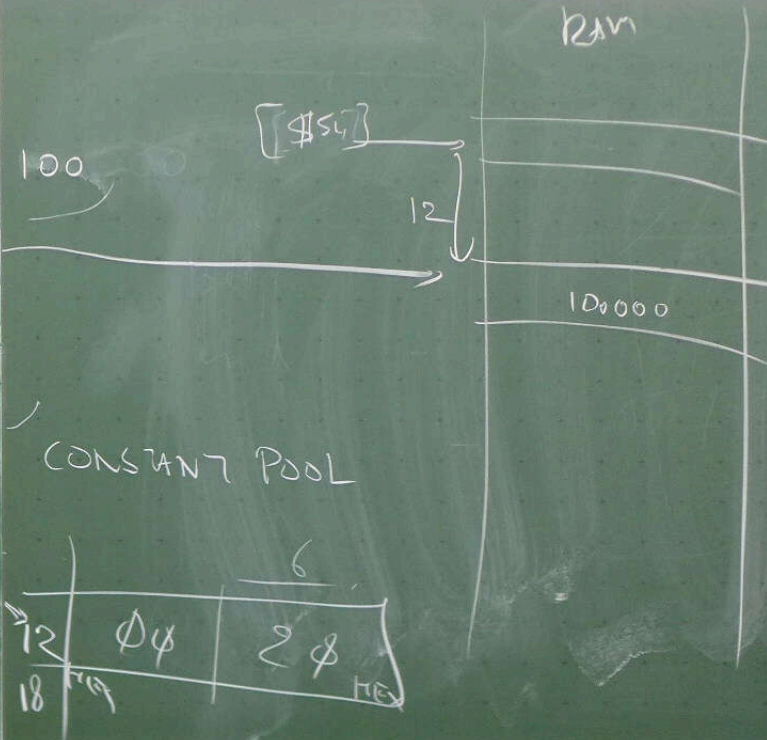
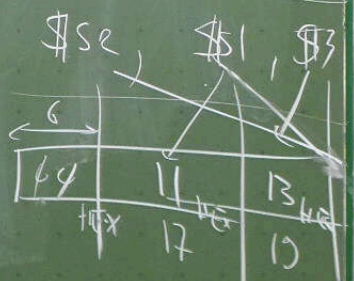
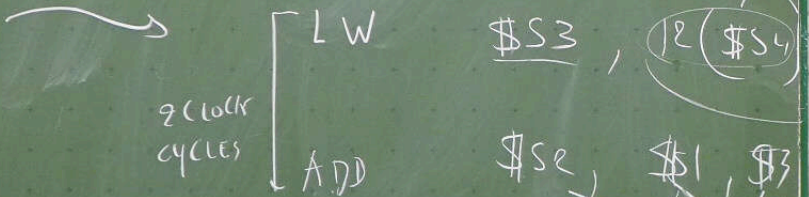
$$\text{OA}[i] = \text{OA}[0] + L * i$$

$$i = i + 1000$$



$$i = i + 100000$$

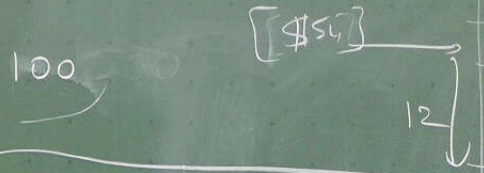
$$[-2^{15}, 2^{15} - 1]$$



$$i = i + 1000$$

1
clock
cycles

ADDI \$S2, \$S1, 1000



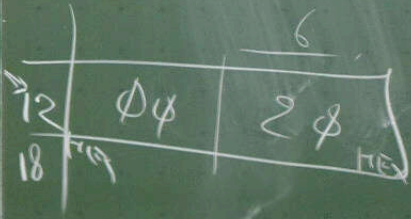
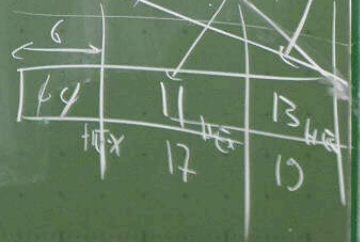
$$i = i + 100000$$

\downarrow
 $[-2^{15}, 2^{15} - 1]$

2
clock
cycles

LW \$S3, 12(\$S4)
 ADD \$S2, \$S1, \$S3

CONSTANT POOL



RAM

10000

ZERO:

ADDI \$ZERO, \$ZERO, 2

PSEUDO CODE

SUBI \$S1, \$S2, 1



ADDI \$S1, \$S2, -1



MIPS INSN (DISASSEMBLE)



ASCII (STRING)



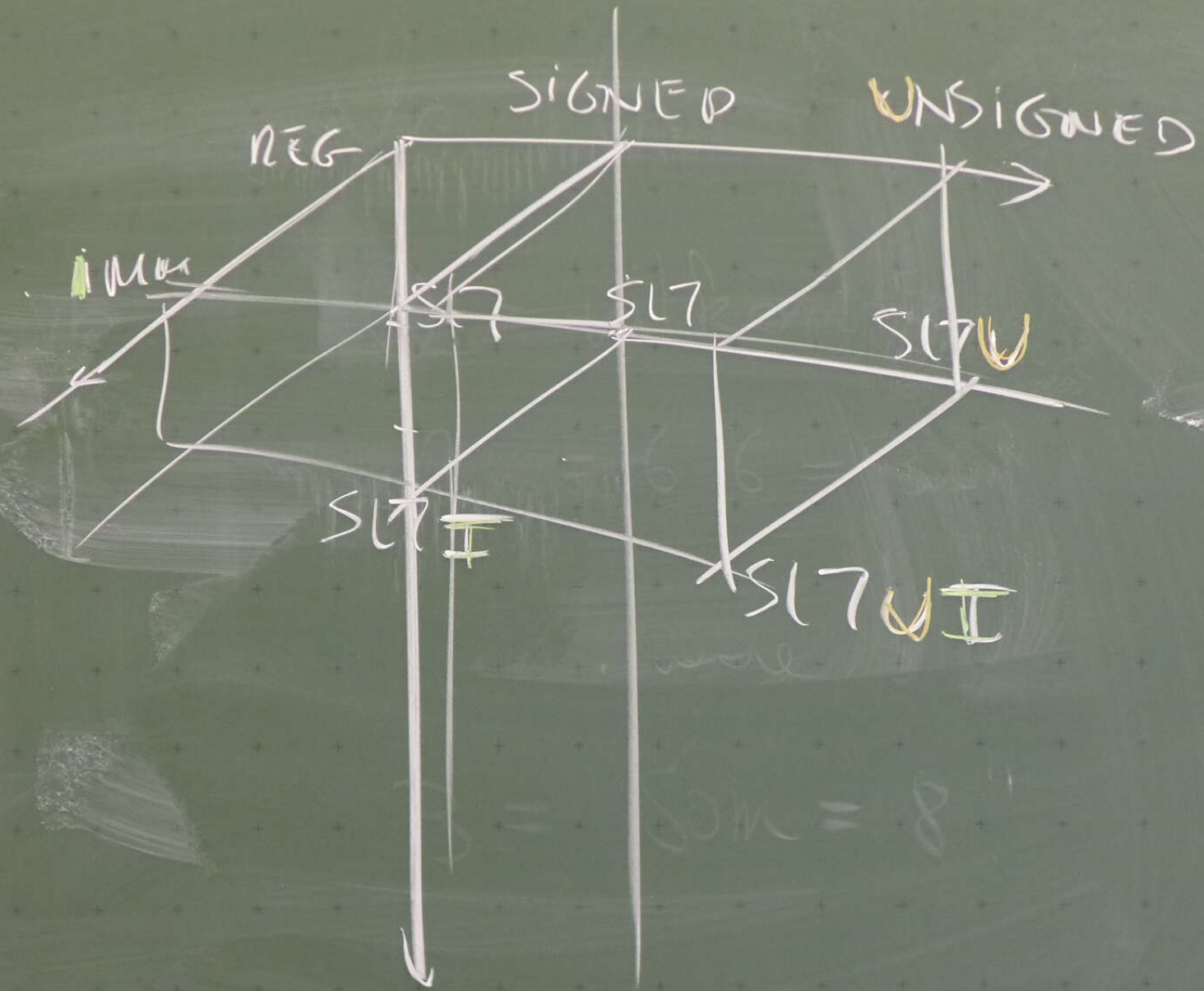
UNSIGNED INT

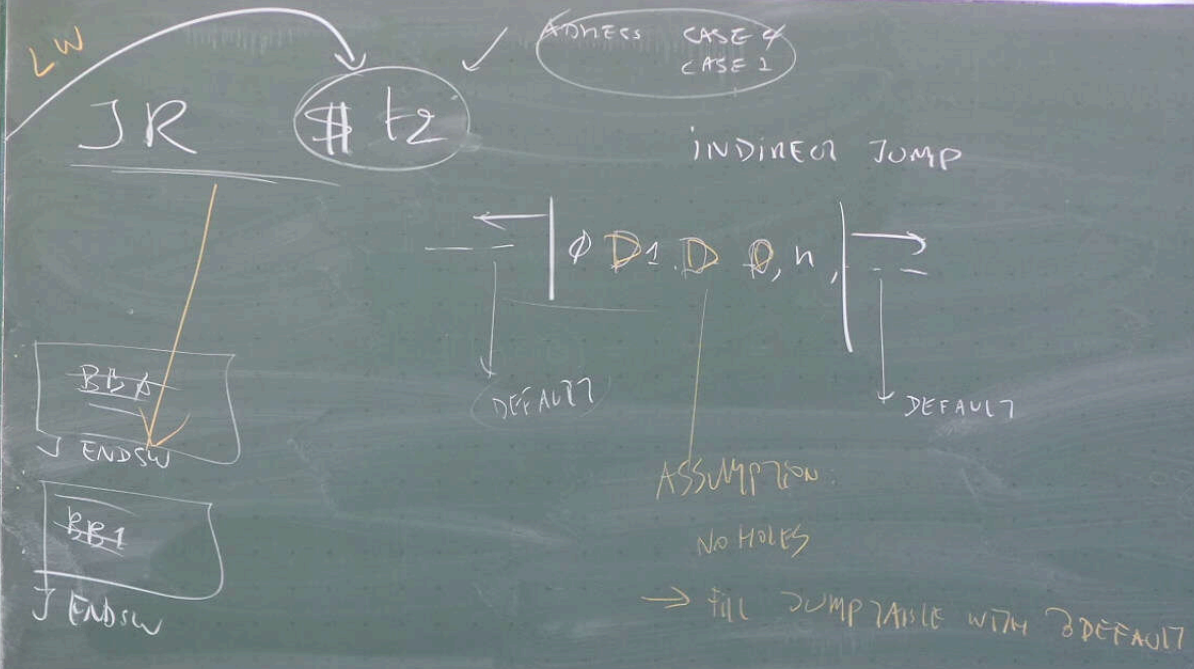
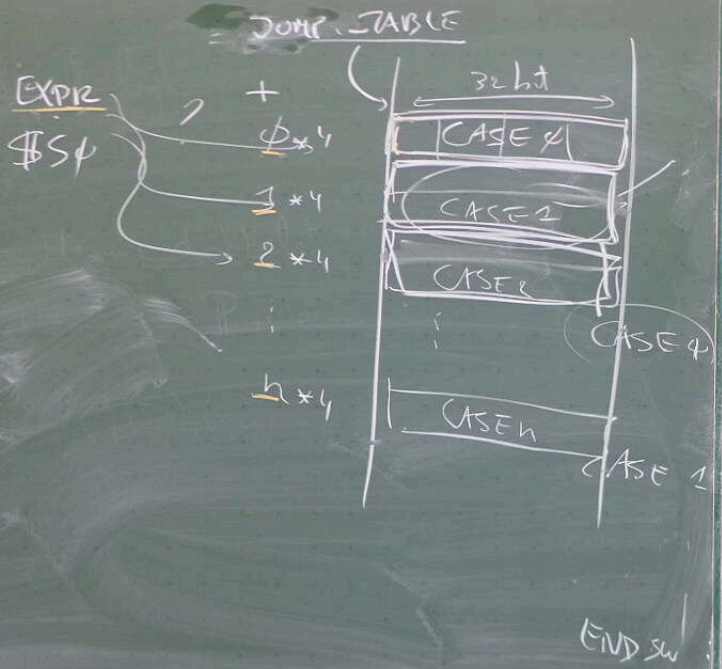


FP

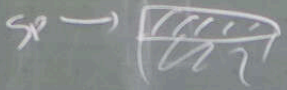


THEORY
EXAMEN

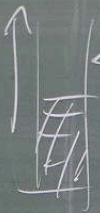
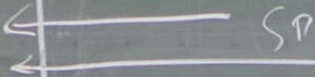
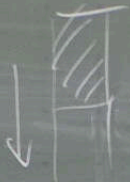
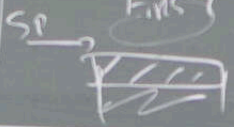




OSP USED

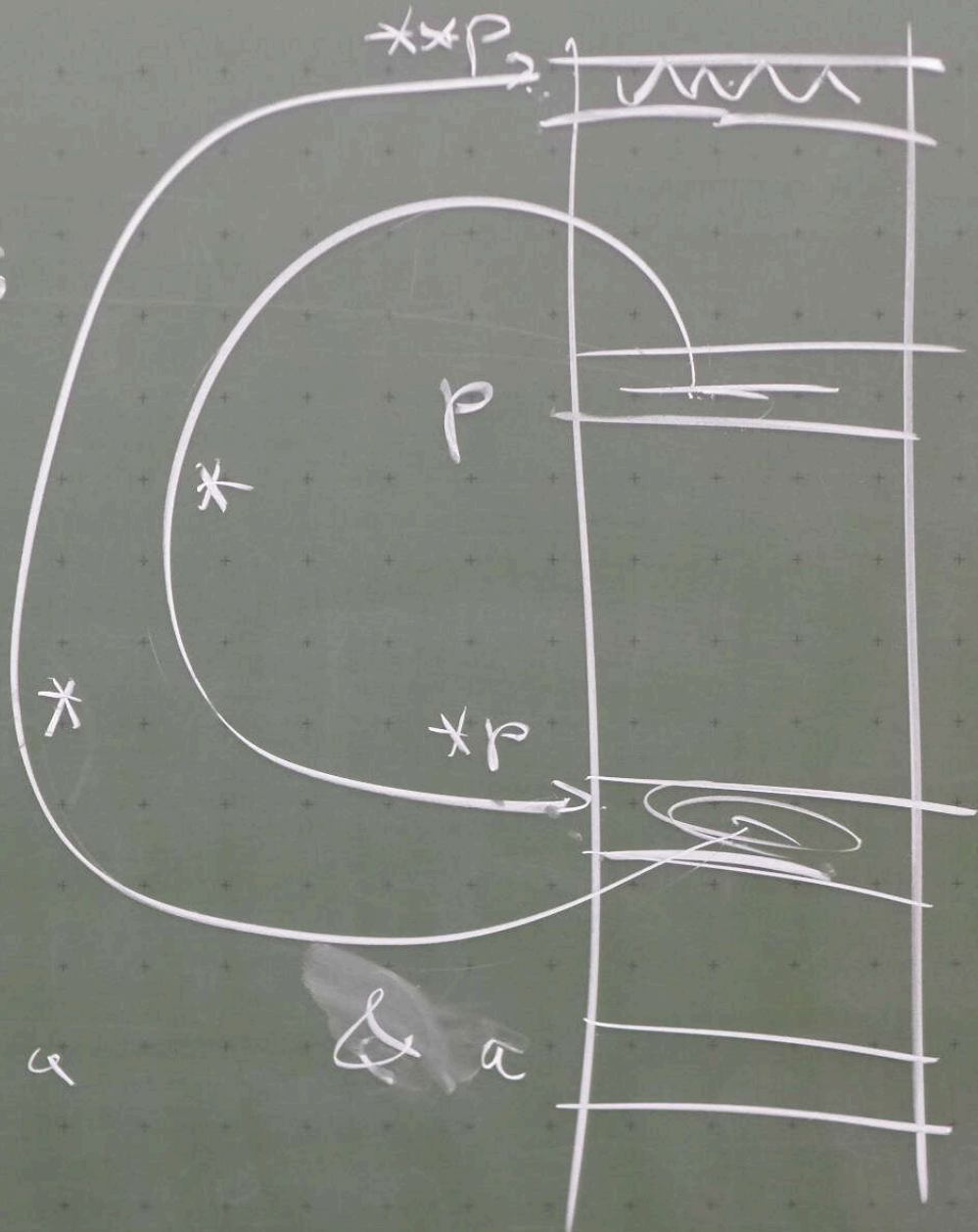


FINS? FREE



int ** p;

int ** [p]



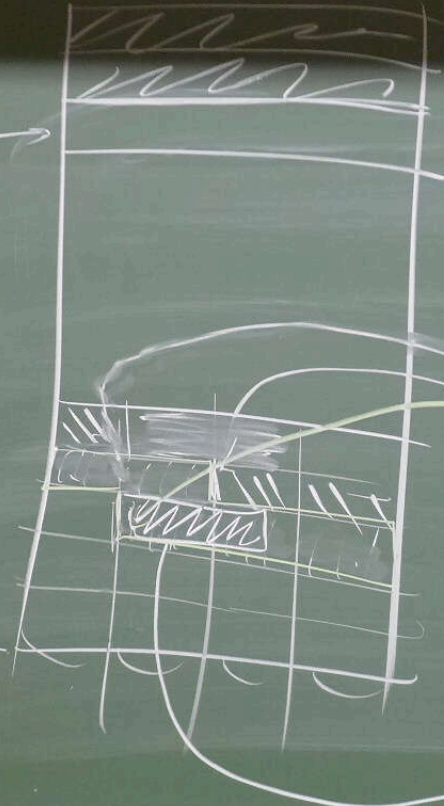
[SP]

STACK

"GARBAGE
COLLECTION"

DEFRAGMENTATION

HEAP BASE ADDRESS

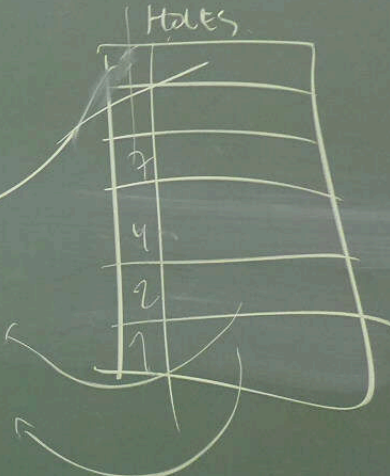


$p = \text{malloc}(5)$

$q = \text{malloc}(3)$

$\text{free}(p)$

$r = \text{malloc}(2)$



main

int f (int i)

int i, j

int g (int l)

int k = 0

k = i + l

return k

i = i + j

i = g(j)

"BINDING"

SCOPE

MATRIX M $R \times K$

ELEMENT TYPE $E1$

LEN($E1$) = EL

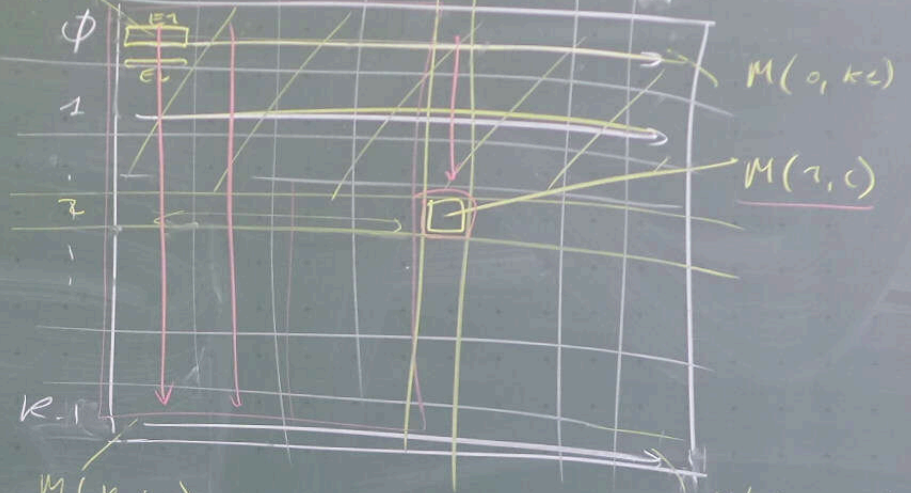
BASE ADDRESS = BA

ADDRESS OF $M(2, c) = ?$

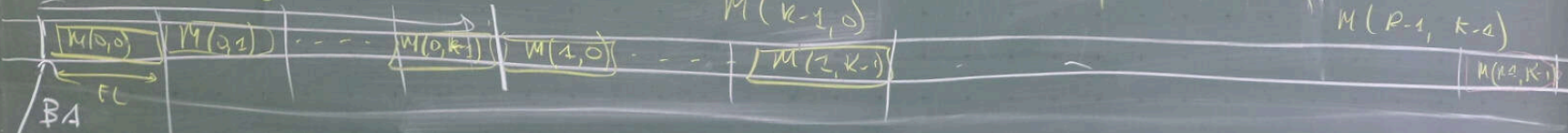
~~$BA + (2 \times K + c) \times EL$~~

~~$BA + (c \times R + 2) \times EL$~~

$M(0,0)$ 0 1 ... c ... $K-1$

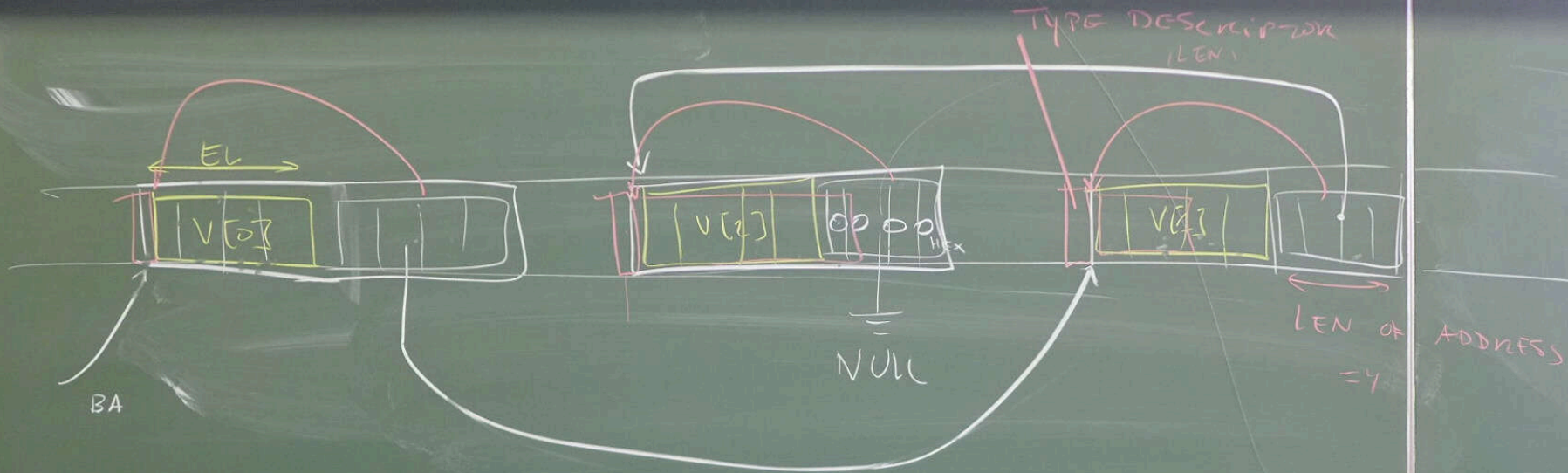


"ROW MAJOR" — C, Java

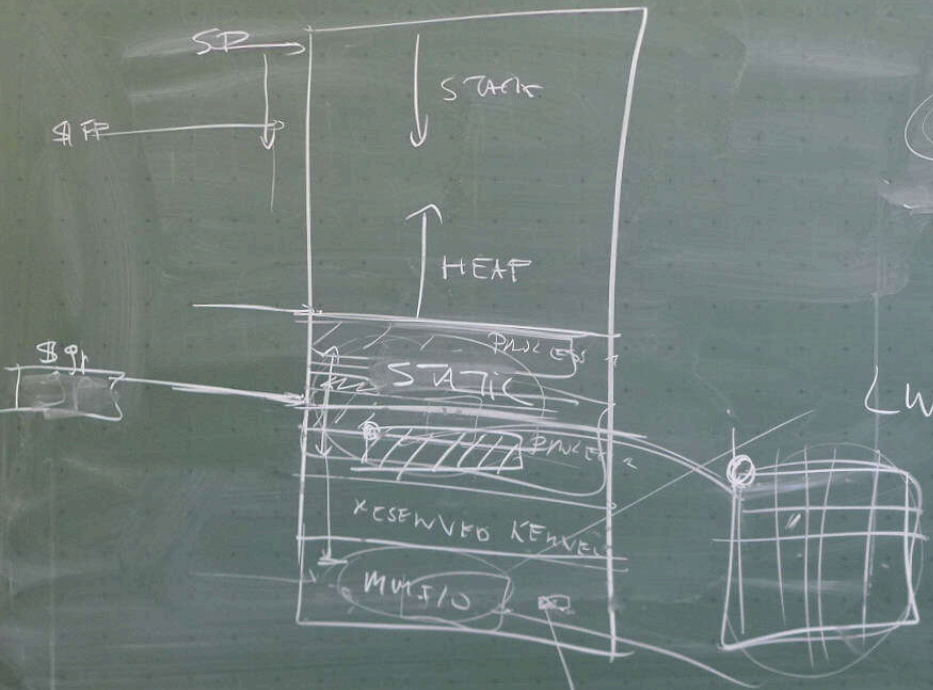


"COLUMN MAJOR" — FORTRAN



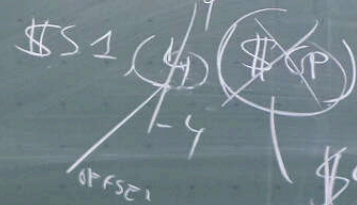


POLYMORPHIC LINKED LIST



$int\ i, j, h$ $STATIC$
 $i = j + h$ $STATIC\ MEM$

$f(m)$
 $\{$
 $\quad int\ i, j, h$
 $\}$
 AUTOMATIC STACK



$ADD\ \$S1, \$GP, \$S2$
 OFFSE1

$x = 1$

$y = 2$

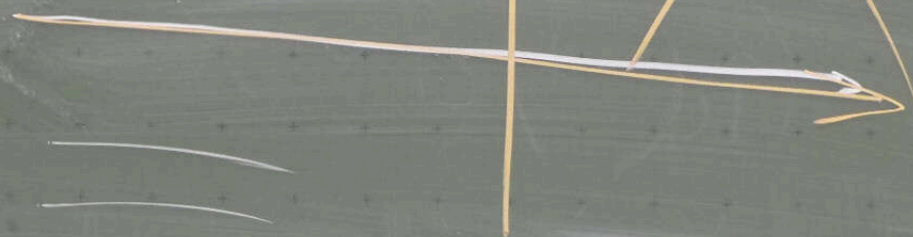
TRUE $1 \neq \emptyset$
FALSE \emptyset

if

$x = y - 1$
1

or

~~$y = 3$~~
3



}