



# Alloy - A lightweight object modelling notation



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# Overview

- Functionality
- Language Definition
- Graphical Syntax
- Based on Z
- Tools
- Extensions
- Conclusion



**“Alloy is a little language for describing structural properties”**

# Functionality

# Functionality

- **Describing of structural properties**
- **Analysis**
  - Simulation (generation)
    - Detect overconstraint
  - Checking (counterexample)
    - Detect underconstraint

# Language Definition

# Language Definition

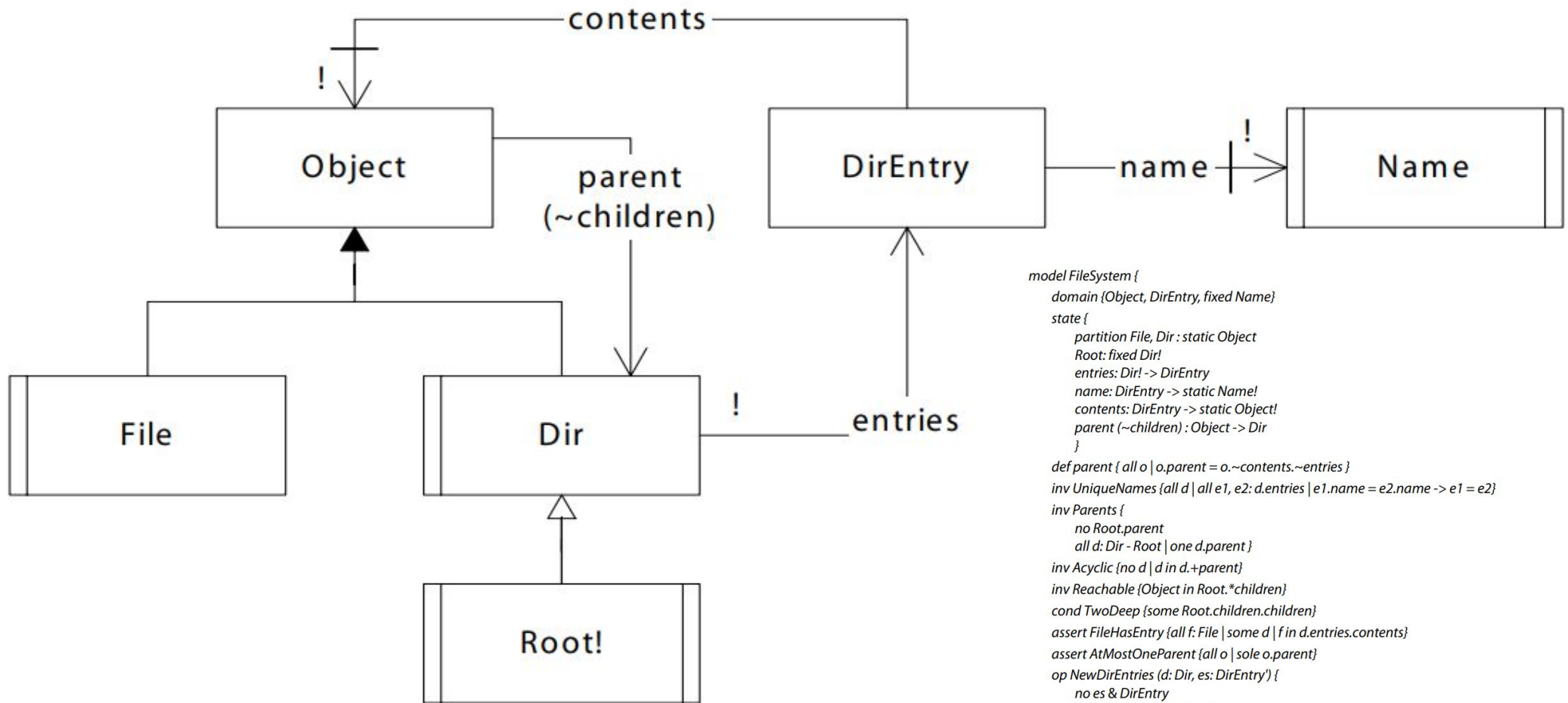
- **Strongly-typed kernel**
- **Singleton-set scalars**
- **Degenerate relation set encoding**
- **Dot operator**
- **Full language**
  - Declarations
  - Shorthands
  - Paragraphs

# Graphical Syntax

# Graphical Syntax

- **State**
- **Constraints**
- **Comparison to UML**





```

model FileSystem {
  domain {Object, DirEntry, fixed Name}
  state {
    partition File, Dir : static Object
    Root: fixed Dir!
    entries: Dir! -> DirEntry
    name: DirEntry -> static Name!
    contents: DirEntry -> static Object!
    parent (~children) : Object -> Dir
  }
  def parent { all o | o.parent = o.~contents.~entries }
  inv UniqueNames {all d | all e1, e2: d.entries | e1.name = e2.name -> e1 = e2}
  inv Parents {
    no Root.parent
    all d: Dir - Root | one d.parent }
  inv Acyclic {no d | d in d.+parent}
  inv Reachable {Object in Root.*children}
  cond TwoDeep {some Root.children.children}
  assert FileHasEntry {all f: File | some d | f in d.entries.contents}
  assert AtMostOneParent {all o | sole o.parent}
  op NewDirEntries (d: Dir, es: DirEntry') {
    no es & DirEntry
    d.entries' = d.entries + es
    all x: Dir - d | x.entries' = x.entries }
  op Create (d: Dir!, o: Object!, n: Name) {
    n lin d.entries.name
    some e: DirEntry' | NewDirEntries (d, e) && e.contents' = o && e.name' = n }
  assert EntriesCreated {all d: Dir, e: DirEntry' | NewDirEntries (d,e) -> DirEntry' = DirEntry + e}
  assert CreateWorks {all d, o, n | Create (d,o,n) -> o in d.children'}
}
  
```

**Based on Z**

# Based on Z

- **Why Z?**
  - Why not OCL?
- **Automatic Analysis**
- **Set-Based Syntax**
- **Mutability**
- **Lexical Issues**

# Tools

# Tools

- **Alcoa: The Alloy Constraint Analyzer**
- **Alloy Analyzer**

# Alcoa: The Alloy Constraint Analyzer

The screenshot shows the ALCOA Alloy Constraint Analyzer interface. The left pane displays the Alloy model code for 'model Bart'. The right pane shows the analysis results, including a table of constraints and a list of relations.

```
model Bart {
  domain (Segment, Connector, Gate, Train)
  state Segments {
    from, to : Segment -> Connector!
    succ : Segment -> Segment
    overlaps : Segment -> Segment
    gate : Segment! -> Gate?
    conflicts : Segment -> Segment
    partition Open, Closed : Gate
    on : Train -> Segment!
  }

  def succ {
    all s | s.succ = {t | t.from = s.to}
  }

  inv Overlaps {
    all s, t | s.from = t.to && s.to = t.from -> s in t.overlaps
    all s | s in s.overlaps
  }
  // all s, t | s in t.overlaps -> t in s.overlaps
  }

  def conflicts {
    all s | s.conflicts = {t | some (s.succ & t.succ.overlaps)} - s
  }

  inv GatePlacement {
    all s | some s.conflicts -> some s.gate
  }

  assert ConflictsSym {
    all s, t | s in t.conflicts -> t in s.conflicts
  }

  inv Policy {
    all s | sole (s.conflicts + s).gate & Open
  }
}
```

inv	op	cond/def	assert
Segments	TrainsMove	succ	ConflictsSym
Overlaps		conflicts	PolicyWorks
GatePlacement		Safety	_assert
Policy		ShowMe	
Separation		ShowMeAcyclic	
		ShowMeConflicts	

Relations:

```
conflicts = {S0 -> {S1,S2}, S1 -> {S0,S2}, S2 -> {S0,S1}}
from = {S0 -> C0, S1 -> C0, S2 -> C2}
gate = {S0 -> C0, S1 -> G1, S2 -> G2}
on = {T1 -> S2, T2 -> S0}
overlaps = {S0 -> {S0,S1}, S1 -> {S1,S2}, S2 -> {S1,S2}}
succ = {S0 -> {S1}, S1 -> {S1}, S2 -> {S1}}
to = {S0 -> C0, S1 -> C0, S2 -> C0}
conflicts' = {}
from' = {S1 -> C0, S2 -> C0}
gate' = {}
on' = {T1 -> S2, T2 -> S1}
overlaps' = {S1 -> {S1,S2}, S2 -> {S1,S2}}
succ' = {}
to' = {S1 -> C0, S2 -> C0}
Skolem constants:
$44 = T2
$45 = T1
s = S2
t = T2
```

Counterexample found (17 seconds)

- Nitpick
- SAT Solver
- Analysis
  - Checks
  - Generation
- Finite scope

File Edit Execute Options Window Help

New Open Reload Save Execute Show

```
// A file system object in the file system
sig FSOBJect { parent: lone Dir }

// A directory in the file system
sig Dir extends FSOBJect { contents: set FSOBJect }

// A file in the file system
sig File extends FSOBJect {}

// A directory is the parent of its contents
fact { all d: Dir, o: d.contents | o.parent = d }

// All file system objects are either files or directories
fact { File + Dir = FSOBJect }

// There exists a root
one sig Root extends Dir {} { no parent }

// File system is connected
fact { FSOBJect in Root.*contents }
```

Solver=sat4j Bitwidth=4 MaxSeq=330 vars. 36 primary vars. 523 cl  
Instance found. Predicate is con

Executing "Run run\$1"  
Solver=sat4j Bitwidth=4 MaxSeq=326 vars. 36 primary vars. 519 cl  
Instance found. Predicate is con

Executing "Run run\$1"  
Solver=sat4j Bitwidth=4 MaxSeq=330 vars. 36 primary vars. 523 cl  
Instance found. Predicate is con

Executing "Check acyclic for 5"  
Solver=sat4j Bitwidth=4 MaxSeq=1124 vars. 67 primary vars. 1915  
No counterexample found. Asser

Executing "Run Default for 4 but 4"  
Solver=sat4j Bitwidth=4 MaxSeq=403 vars. 41 primary vars. 516 cl  
Instance found. Predicate is con

Executing "Run run\$1"  
Solver=sat4j Bitwidth=4 MaxSeq=330 vars. 36 primary vars. 514 cl  
Instance found. Predicate is con

Executing "Run run\$1"  
Solver=sat4j Bitwidth=4 MaxSeq=326 vars. 36 primary vars. 510 cl  
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Solver=sat4j Bitwidth=4 MaxSeq=326 vars. 36 primary vars. 510 cl  
Instance found. Predicate is con

Executing "Run Default for 4 but 4"  
Solver=sat4j Bitwidth=4 MaxSeq=403 vars. 41 primary vars. 516 cl  
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Line 20, Column 36 [modified]

# Alloy Analyzer

(Trolley) Run Default for 4 but 4 int, 4 seq expect 1

File Instance Theme Window

Projection: none

contents: 3  
parent: 3

Root

File0

File1

Dir

parent

contents

parent

contents

parent

contents

(Trolley) Run Default for 4 but 4 int, 4 seq expect 1

File Instance Theme Window

General Graph Settings:

Node Color Palette: Martha Use original atom names:

Edge Color Palette: Classic Font Size: 12

Hide private sigs/relations:

Hide meta sigs/relations:

general graph settings

types and sets

- sig univ
  - sig FSOBJect
    - sig Dir extends FSOBJect
      - sig Root extends Dir
      - sig File extends FSOBJect
    - sig Int
      - sig seq/Int extends Int
      - sig String

relations

- contents : Dir -> FSOBJect
- parent : FSOBJect -> Dir

Root

Dir

File0

File1

parent

contents

parent

contents

parent

contents

File Edit Execute Options Window Help

ZZZ vars Instance

```

sig Class {
  students: set Student
}

sig Student {
  attends: Class
}

fact {
  all s: Student, c: s.attends | s in c.students
  all c: Class, s: Student | s in c.students => s.attends = c
}

```

Starting th  
A type err  
This canno  
left hand s  
right hand

Starting th  
A syntax e  
The name

(Class) Run Default for 4 but 4 int, 4 seq expect 1

File Instance Theme Window

Viz Txt Table Tree Theme Magic Layout Evaluator New Projection: none

attends: 4  
students: 4

Student2

Class0

Class2

Class1

Student0

Student1

Student3

students attends

students attends

students attends

students attends

students attends

students attends

ZZZ vars Instance

# Alloy Analyzer

(Trolley) Run Default for 4 but 4 int, 4 seq expect 1

File Instance Theme Window

Viz Txt Table Tree Theme Magic Layout Evaluator New Projection: none

contents: 3  
parent: 3

Root

File0

File1

parent contents

parent contents

parent contents

parent contents

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types and sets

- sig univ
  - sig FSOBJECT
    - sig Dir extends FSOBJECT
      - sig Root extends Dir
      - sig File extends FSOBJECT
    - sig Int
      - sig seq/Int extends Int
      - sig String

relations

- contents : Dir -> FSOBJECT
- parent : FSOBJECT -> Dir

Root

Dir

File0

File1

parent contents

parent contents

parent contents

parent contents



# Extensions

# Extensions

- Alloy\*
- Electrum
- Aluminum

# Conclusion

