Finding and fixing bugs in model transformations with formal verification: An experience report

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Abstract

We report on the use of a formal verification tool for a graph-based transformation language in the context of a case study. The tool identified two bugs in the transformation that had eluded all previous testing efforts. The paper describes what we learned about the analysis of model transformations and how we intend to use these insights to improve the verification tool.

1 Introduction

In Model-Driven Development (MDD), model transformations are used to automate MDD tasks such as querying, model extraction, and code generation [LAD15]. A model transformation is a program that maps input models (conforming to a source metamodel) into their corresponding output models (conforming to a target metamodel). The ability to identify and avoid bugs in model transformations is very beneficial to MDD in general, and to the successful application of MDD for safety-critical software in particular.

In this paper, we report on our experiences using a tool that we have recently developed for the formal verification of model transformations [SLC14, Sel15]. The tool analyzes transformations expressed in a graph-based transformation language called DSLTrans with respect to pre- and post-condition pairs. We use this tool for the analysis of an existing model-to-model transformation that transforms state machine models expressed in the UML profile UMLRT [Sel98], to equivalent models in Kiltera [PD10a], a timed extension of the π-calculus.

The contributions of this experience report are two-fold: (1) We summarize some observations that are, hopefully, of value to practitioners developing model transformations and researchers working on quality assurance techniques for model transformations; some of these observations speak to known problems such as the subtleties and limitations of testing and the dangers of refactoring, while other observations are more technical and identify, for example, different kinds of properties that we found useful. (2) We describe how the case study has influenced our plans for future work on our DSLTrans verification tool and further advancing the state-of-the-art in model transformation verification.

The rest of this paper is organized as follows: Section 2 describes the UMLRT-to-Kiltera case study. Section 3 overviews DSLTrans and our property prover. Section 4 demonstrates the verification results. Section 5 discusses the lessons learned. Section 6 summarizes related work. Section 7 concludes the study.

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2 The UML-RT-to-Kiltera Model Transformation: Problem Description

Model transformations are used to achieve many tasks in MDD, one of which is facilitating the analysis of models by translating models into an analyzable language in such a way that analysis results are preserved [LAD+15].

UML-RT [Sel98] is a UML profile that has been used in many industrial sectors (e.g., telecommunication) for the development of event-driven, soft real-time systems. It is supported by commercial MDD tools such as IBM RSA-RTE [IBM] and the open-source tool Papyrus-RT [Fon]. To enable the analysis of UML-RT models, Posse and Dingel recently developed a translation of UML-RT state machine diagrams and capsule diagrams into a language called Kiltera [PD14].

Kiltera [PD10a] is a language for expressing, simulating, and analyzing systems that are either concurrent or distributed. Kiltera allows for code to be executed in different, dynamically changing locations, and supports a notion of time that influences execution behaviour. A Kiltera program consists of processes that communicate asynchronously over channels. Its formal semantics is based on a timed extension of the \( \pi \)-calculus [PD10b].

As in the \( \pi \)-calculus, channels can be sent as parts of messages which allows for the easy implementation of, for example, call-backs by providing a called process with a “handle” to be used to send computation results back to the caller; interestingly, the passing of channel names allowed for the dynamic aspects of UML-RT (such as optional and dynamic capsules) to be captured succinctly and cleanly.

Paen [Pae12] has implemented a mapping of UML-RT state machines into Kiltera process models [PD14] as an ATL model transformation. We refer to this transformation as the UML-RT-to-Kiltera model transformation. We summarize a subset of the source and target metamodels of the UML-RT-to-Kiltera transformation that are relevant to this paper.

2.1 The Source UML-RT metamodel

In UML-RT, a system’s structure is specified as a capsule diagram composed of system components or capsules. The behavior of these capsules is specified using state machine diagrams (e.g., Fig. 1). We discuss the concepts of UML-RT metamodel by stating class names (which correspond to UML-RT concepts) in italics, and referring to examples of these concepts in Fig. 1.

A UML-RT state machine has one or more (hierarchical) States, for example, states ‘n2’ and ‘n3’ in Fig. 1. States are traversed through Transitions, such as transition ‘t1’ in Fig. 1. Transitions can be sibling transitions between states in the same hierarchical level, incoming transitions from a state to one of its sub-states, outgoing transitions from a sub-state to its containing state, or initial transitions from a state’s InitialPoint (e.g., ‘init1’ in Fig. 1) to one of its sub-states (classes SIBLING0, IN1, OUT2, and association initialTransition). Transitions can have Triggers, where each trigger is composed of a Signal received on a Port. For example, transition ‘t1’ in Fig. 1 is triggered by signal ‘sig1’ on port ‘p1’. A transition crossing state boundaries is broken into segments, where each segment links EntryPoints (e.g., ‘a1’ in Fig. 1) and/or ExitPoints (e.g., ‘b1’ in Fig. 1).

2.2 The Target Kiltera Metamodel

Next we introduce the concepts of the Kiltera metamodel considered by Posse and Dingel [PD14]. Kiltera includes five classes of constructs: expressions (class Expr), patterns (class Pattern), guards (Class ListenBranch), definitions (Class Def), and processes (class Proc). Expressions and patterns can be constants, variables, and tuples. Expressions also include function calls. Table 1 enumerates a subset of the guards, definitions, and processes relevant to this study (including their syntax and their corresponding classes from the Kiltera metamodel). We discuss the semantics of these Kiltera constructs in the following.

A process definition of the form \( \text{proc}\ A(x_1, \ldots, x_n) = P \) defines a process \( A \) with parameters \( x_i \) that are used in the body of the process \( P \). Thus, the instantiation process \( A(E_1, \ldots, E_n) \) instantiates a process defined by \( \text{Proc}\ A(x_1, \ldots, x_n) = P \) where the parameters \( x_i \) are substituted in \( P \) by the values of the expressions \( E_i \). The process done represents a successfully terminated process. A trigger (i.e., \( \alpha E \)) outputs the value of expression \( E \) over channel \( \alpha \). In listener processes (i.e., when \( [G_1 \rightarrow P_1|\ldots|G_n \rightarrow P_n] \)), \( G_i \) is an input guard which takes the form \( a_i \lnot R_i @ y_i \), where \( a_i \) is a channel, \( R_i \) is a pattern, and \( y_i \) is a variable. A listener listens to channels \( a_i \) of the guards \( G_i \). When a channel \( a_i \) is triggered with a value matching the pattern \( R_i \) of guard \( G_i \), three steps are carried out: (1) process \( P_i \) is executed, (2) variable \( y_i \) of guard \( G_i \) stores the time waited by the listener, and (3) the alternative guards are ignored. The new process (i.e., \( \text{new}\ a_1, \ldots, a_n \ in P \)) creates the channels \( a_i \) that are private to process \( P \). Conditionals have the standard semantics. Local definitions (i.e., def\( \{D_1; \ldots; D_n\}\) in \( P \)) declare the definitions \( D_i \) and executes \( P \), where the scope of \( D_i \) is the entire term. Parallel and sequential processes represent the parallel and sequential composition of the processes in the term.
Table 1: The names of Kiltera’s constructs, their syntax, and their representative classes

<table>
<thead>
<tr>
<th>Name</th>
<th>Syntax</th>
<th>Corresponding class from Fig. 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>Input Guards</td>
<td>a?R@y</td>
<td>Class ListenBranch : attributes channel and after and an association to class Pattern represent a, y, and R in a?R@y</td>
</tr>
<tr>
<td>Process Definition</td>
<td>proc A(x1,...,xn)=P</td>
<td>Class ProcDef : attribute name and associations with classes Name and Proc represent A, x1, and P in proc A(x1,...,xn)=P</td>
</tr>
<tr>
<td>Termination Process</td>
<td>done</td>
<td>Class Null</td>
</tr>
<tr>
<td>Trigger Process</td>
<td>a!E</td>
<td>Class Trigger : attribute channel and association with class Expr represent a and E in a!E</td>
</tr>
<tr>
<td>Listener Process</td>
<td>When(GL→P1,...,Gn→Pn)</td>
<td>Class Listen : associations with classes ListenBranch and Proc represent Gi and Pi in When (GL→P1,...,Gn→Pn)</td>
</tr>
<tr>
<td>New Process</td>
<td>New a1,...an in P</td>
<td>Class New : associations with classes Name and Proc represent ai and P in New a1...an in P</td>
</tr>
<tr>
<td>Conditional Process</td>
<td>if E then P1 else P2</td>
<td>Class ConditionSet : associations with classes ConditionBranch and Proc represent the “if” clause and the “else” clause.</td>
</tr>
<tr>
<td>Instantiation Process</td>
<td>A(E1,...,En)</td>
<td>Class Inst : attribute name and association with class Name represent A and Ei in A(E1,...,En)</td>
</tr>
<tr>
<td>Local Definition Process</td>
<td>def(D1),...,Dn; in P</td>
<td>Class LocalDef : associations with classes Def and Proc represent Di and P in def(D1),...,Dn; in P</td>
</tr>
<tr>
<td>Parallel Composition Process</td>
<td>P1;P2</td>
<td>Class Par : association with class Proc represent Pi in P1;P2</td>
</tr>
<tr>
<td>Sequential Composition Process</td>
<td>P1;P2</td>
<td>Class Seq : associations with class Proc represent Pi in P1;P2</td>
</tr>
</tbody>
</table>

2.3 The UML-RT-to-Kiltera Model Transformation Mapping Rules

Due to space limitations, we describe the required mapping informally, using the examples shown in Figs. 1 and 2. The detailed mapping rules between the UML-RT and Kiltera metamodels are described in [PD14].

Fig. 1 shows a state machine with one composite state n2 and Fig. 2 shows the equivalent Kiltera mapping of state n2. The UML-RT-to-Kiltera transformation, in general, maps (a) any state n to a Kiltera process definition named Sn, (b) the entering of a state n to an instantiation of Kiltera process Sn, and (c) signals of transitions’ triggers to Kiltera channels in the output. Thus, the composite state n2 in Fig. 1 is mapped to a process definition Sn2 (Fig. 2) with some parameters. Sub-states n3 and n4 of state n2 are mapped to nested process definitions Sn3 and Sn4 of process Sn2 (line 3 of Fig. 2).

To encode transitions with triggers for state n2, process Sn2 has a sub-process Handler (lines 9-15 in Fig. 2) which is a listener process that handles all events of state n2. For example, one branch of the Handler subprocess waits for input on channel sig1 (representing waiting for the reception of sig1) by state n2. Once an input is received, the Handler sends an exit request to state n2’s active sub-state on the exit’ channel. When the sub-state sends an acknowledgement on the exack’ channel, the Handler ‘instantiates’ process Sn1 corresponding to the transition’s target state n1.

When state n2 is entered, the choice of the sub-state to enter next is encoded using sub-process Dispatcher of process Sn2 (lines 6-8 in Fig. 2). If state n2 is entered through entry point a1 (identified by the argument passed to parameter exp of the Dispatcher) that is connected to sub-state n4, then the Dispatcher instantiates Sn4. If, however, state n2 is entered through an entry point that is not explicitly connected to a sub-state, then the Dispatcher follows state n2’s initial transition and enters the initial sub-state (i.e., instantiates Sn3).

Exit point b1 of state n2 is mapped to a sub-process Bn2 of process Sn2. Subprocess Bn1 executes two steps in parallel: (1) triggers a stop handler request on channel sh (short for stop handler), and (2) instantiates process Sn1 corresponding to the target state n1 of the transition leaving the exit point.

3 Background

We briefly overview the DSLTrans model transformation language, the property prover we built for verifying DSLTrans transformations, and properties that are provable using our prover.

3.1 The DSLTrans Model Transformation Language

DSLTrans [BLA11] is a graphical model transformation language that is Turing incomplete, i.e., DSLTrans can not specify unbounded loops. Transformations built using DSLTrans are confluent and terminating by construction. In DSLTrans, a transformation is composed of a set of ordered layers that are executed sequentially. A layer contains one or more transformation rules that execute in a non-deterministic order but produce a deterministic result. Each rule is a pair (MatchModel, ApplyModel) where the MatchModel/ApplyModel is a
pattern of source/target metamodel elements (called match/apply elements in DSLTrans). Match elements can be of two types: Any match elements are bound to all matching instances in the input model, and Exists match elements are bound to only one matching instance in the input model.

Fig. 3 shows an example of a DSLTrans rule (called ‘State2ProcDef’) from the first layer of the UML-RT-to-Kiltera transformation. The MatchModel of the ‘State2ProcDef’ rule has a ‘State’ element of type Any from the UML-RT metamodel and the ApplyModel has one ‘ProcDef’ element and three ‘Name’ elements from the Kiltera metamodel. This means that every ‘State’ input model element will be transformed into a ‘ProcDef’ output model element connected to three ‘Name’ elements (with literals exack, exit, and enp). The attribute name of the ‘ProcDef’ element is the concatenation of S and the name of the State element in the MatchModel. When a DSLTrans rule executes, traceability links are created between each element in the rule’s MatchModel and each element in the ApplyModel. These keep track of which output elements came from which input elements.

Rule ‘MapBasicStateNoTrans’ in Fig. 4 shows three additional DSLTrans constructs: attribute conditions on match elements, free variables, and backward links. Attribute conditions on match elements (e.g., the conditions on the attributes ‘isComposite’ and ‘hasOutgoingTransitions’ of the ‘State’ match element in Fig. 4) act as a filter on the matching process, where only ‘State’ elements fulfilling these attribute conditions are matched. DSLTrans uses free variables and backward links to allow a rule to refer to a specific element that has already been created in a previous layer.

The two rules in Figs. 3 and 4 show an example of how free variables and backward links are used, where (i) both rules have a free variable with a value of ‘procdef’ in the apply element ‘ProcDef’, and (ii) rule ‘MapBasicStateNoTrans’ has a backward link appearing as a vertical dashed line between the ‘ProcDef’ apply element and the ‘State’ match element. The first occurrence of the free variable ‘procdef’ (without a backward link) in rule ‘State2ProcDef’ (Fig. 3) of the first transformation layer binds the ‘procdef’ variable to the ‘ProcDef’ element.
<table>
<thead>
<tr>
<th>Layer</th>
<th>Rule Name</th>
<th>Input Types</th>
<th>Output Types</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>State2ProcDef</td>
<td>State</td>
<td>ProcDef, Name</td>
</tr>
<tr>
<td>2</td>
<td>MapBasicStateNoTrans</td>
<td>State</td>
<td>ProcDef, Null</td>
</tr>
<tr>
<td></td>
<td>MapBasicState</td>
<td>State</td>
<td>ProcDef, Listen, ListenBranch, Trigger</td>
</tr>
<tr>
<td></td>
<td>MapCompositeState</td>
<td>State</td>
<td>ProcDef, LocalDef, New, Par, Inst, Name</td>
</tr>
<tr>
<td>3</td>
<td>ExitPoint2ProcDef</td>
<td>State, ExitPoint</td>
<td>LocalDef, ProcDef, Name, Par, Trigger</td>
</tr>
<tr>
<td></td>
<td>State2Handler</td>
<td>State</td>
<td>LocalDef, ProcDef, Name, Listen, ListenBranch, Null, Seq, Trigger</td>
</tr>
<tr>
<td></td>
<td>State2Dispatcher</td>
<td>State, Transition, EntryPoint, StateMachine</td>
<td>LocalDef, ProcDef, Name, ConditionSet, Inst</td>
</tr>
<tr>
<td>4</td>
<td>Trans2InstSIB</td>
<td>Transition, Vertex, StateMachine, SIBLING0</td>
<td>Inst, Name</td>
</tr>
<tr>
<td></td>
<td>Trans2InstOUT</td>
<td>Transition, StateMachine, Vertex, OUT2</td>
<td>Inst, Name</td>
</tr>
<tr>
<td></td>
<td>Trans2Inst</td>
<td>State, Transition, EntryPoint, StateMachine, IN1</td>
<td>Inst, Name</td>
</tr>
<tr>
<td></td>
<td>Trans2ListenBranch</td>
<td>State, Transition, Trigger, Signal</td>
<td>Listen, ListenBranch, Inst</td>
</tr>
<tr>
<td></td>
<td>MapExitWithTrans</td>
<td>ExitPoint, Transition</td>
<td>Par, Inst</td>
</tr>
<tr>
<td></td>
<td>Trans2HListenBranch</td>
<td>State, Transition, Vertex, StateMachine, Trigger, Signal</td>
<td>Listen, ListenBranch, Seq, Trigger, Inst</td>
</tr>
<tr>
<td>5</td>
<td>MapStatesINtrans</td>
<td>State, Transition, IN1, Vertex</td>
<td>ConditionSet, ConditionBranch, Expr, Inst</td>
</tr>
<tr>
<td>6</td>
<td>MapNesting</td>
<td>State</td>
<td>LocalDef, ProcDef</td>
</tr>
</tbody>
</table>

Table 2: The rules in each layer of the UML-RT-to-Kiltera transformation and their input and output types generated by the rule. Any occurrences of the free variable ‘procdef’ in successive layers with backward links (e.g., in rule ‘MapBasicStateNoTrans’ of the second transformation layer shown in Fig. 4) matches only previously generated ‘ProcDef’ elements that have been bound to the same free variable ‘procdef’. Thus, rules with apply elements that are not connected by backward links (e.g., ‘ProcDef’ element of rule ‘State2ProcDef’ in Fig 3) create output elements of the same type each time the MatchModel of the rule is found in the input. However, apply elements that are connected by backward links (e.g., ‘ProcDef’ element of rule ‘MapBasicStateNoTrans’ in Fig 4) are used to match an element that has been previously created.

3.2 DSLTrans Implementation of the UML-RT-to-Kiltera Transformation

Table 2 summarizes the rules in each layer of the UML-RT-to-Kiltera transformation, and the input/output types that are mapped/created by each rule. The complete DSLTrans implementation of the transformation is demonstrated in [Sel15].

3.3 DSLTrans Symbolic Model Transformation Property Prover

Fig. 5 demonstrates the architecture of our property prover [SLC+14], now called SyVOLT. Our prover takes four inputs: the DSLTrans transformation of interest, the transformation’s source and target metamodels, and the property to verify. Verification is then carried out in two steps, as shown in Fig. 5.

In the first phase, the prover generates the set of path conditions representing all possible symbolic executions of the input transformation. Each path condition is generated by accumulating a possible combination of rules that can be triggered by some input model. We refer to the accumulated MatchModels (or ApplyModels) of all the rules in a path condition as the path condition’s match pattern (or apply pattern). The path condition generation algorithm is explained in detail in [LOV14].

In the second phase, the prover verifies the input property on each path condition generated in the first phase. The prover renders the property to be either true (if the property holds for each of the generated path conditions) or false with a counter example (if the property does not hold for at least one path condition). Our property prover is input-independent [ALS+12], i.e., property verification is performed once for the transformation and the verification result is guaranteed to hold for the transformation when run on any input model.

![Figure 5: The architecture of our symbolic model transformation property prover.](image-url)
Three property types can be expressed and verified using our property prover: AtomicContracts, propositional formulae on AtomicContracts, and rule reachability. For this study we focus only on the first two property types.

An AtomicContract is a pair \((pre, post)\) that specifies a property of the form: “if the input model satisfies the precondition \(pre\), then the output model should satisfy the postcondition \(post\)”. A (pre- or) postcondition is a constraint on the (input or) output model of the transformation in the form of a structural relation between (input or) output model elements. Pre- and postconditions are expressed using the same constructs as rules (described in Section 3.1). Postconditions may also have traceability links to link postcondition elements to precondition elements. Traceability links in postconditions signify that the property will only match an output model element that was previously created from (and hence, linked to) the input model element.

Fig. 6 demonstrates an AtomicContract AC1 used to express a property (referred to as \(P1\)) of the UML-RT-to-Kiltera transformation. AC1 (Fig. 6) is interpreted as: “two nested States in the input will always be transformed to two nested ProcDef s in the output”. Using three traceability links in Fig. 6 (appearing as three vertical, dashed lines) mandates that AC1 will only match ProcDef and LocalDef elements that were previously created from State elements. Our property prover should prove that AC1 will always hold for the UML-RT-to-Kiltera transformation.

AtomicContracts can be composed using standard propositional connectives. For instance, the implication ‘\(AC2 \implies AC3\)’ in (Fig. 7) captures the ‘2..*’ multiplicity invariant (referred to as \(M1\))\(^1\): In the output, every Par element (i.e., a parallel composition) is associated with two or more Proc elements (i.e., processes) through the association \(p\). More precisely, if an element of type ‘Par’ (referred to as variable ‘PAR’) is generated in the output (again as variable ‘PAR’) in AC2, then this element must be connected to at least two ‘Proc’ elements.

4 Testing and Verification of the UML-RT-to-Kiltera Model Transformation

We begin by briefly describing how the transformation was tested during its development (Section 4.1). We then identify some relevant properties that the transformation should satisfy to be considered correct (Section 4.2). The application of our property prover to the transformation then follows (Section 4.3).

4.1 Testing

The transformation was extensively unit tested using the following process: Each time a rule was created, appropriate input models to test that rule were created depending on the complexity of the rule. If the rule produced the expected output, development would proceed with the next rule; otherwise, the rule would be debugged. In total, the transformation was tested on 25 different input models, none of which revealed any bugs.

4.2 Properties of Interest

We divide the desired properties of the UML-RT-to-Kiltera transformation into four categories: pattern contracts, multiplicity invariants, syntactic invariants, and rule reachability. Contracts are properties that relate elements of the source and target metamodels, and are expressed using AtomicContracts. Invariants are properties defined on elements of the target metamodel only, and are expressed using propositional formulae of AtomicContracts.

\(^1\)Note that the two AtomicContracts in Fig. 7 have empty preconditions meaning that they will match on any input model.
Figure 8: AtomicContracts $AC4$ and $AC5$ that are used to express a syntactic invariant as $AC4 \Rightarrow AC5$.

We summarize the four property categories and we demonstrate how exemplar properties from the four categories are formulated in our prover. The property categories are described in detail in [Sel15].

**Pattern contracts** require that if a certain pattern of elements exists in the input model, then a corresponding pattern of elements exists in the output model. For example, pattern contract $P1$ (Section 3.4, Fig. 6) ensures that “two nested States in the input will always be transformed to two nested ProcDefs in the output”.

**Multiplicity invariants** ensure that the transformation does not produce an output that violates the multiplicities in the target Kiltera metamodel. For example, multiplicity invariant $M1$ (discussed in Section 3.4, Fig. 7) ensures that each output Par element is associated to two or more Proc elements through the $p$ association.

**Syntactic invariants** ensure that the generated Kiltera output is well-formed with respect to Kiltera’s syntax. An example of a syntactic invariant (referred to as $S1$) ensures that if a process named Dispatcher is instantiated, then a process named Dispatcher is also defined. Using the AtomicContracts in Fig. 8, $S1$ can be expressed as $AC4 \Rightarrow AC5$. The former propositional formula can be interpreted as “If the output has an Inst element named Dispatcher ($AC4$), then the output must have the same Inst element accompanied with a ProcDef element named Dispatcher ($AC5$)”. The free variable ‘INST’ in Fig. 8 mandates that if $AC4$ holds for a specific Inst element, then $AC5$ should also hold for the same Inst element.

**Rule reachability** checks whether a specific rule can be triggered in any path condition of the transformation. A rule that is not reachable is said to be a dead rule and indicates a transformation bug that needs to be fixed.

We defined and formulated 11 multiplicity invariants, 3 syntactic invariants, 5 pattern contracts, and 15 rule reachability checks (for each of the 15 rules summarized in Table 2).

### 4.3 Verification

We used our property prover to verify these properties for the UML-RT-to-Kiltera transformation.

#### 4.3.1 Performance

The first phase of the verification, the generation of the path constraints (Figure 5), completed in less than 14 seconds\(^2\) and resulted in 57 different path conditions, i.e., 57 different feasible sequences of rule applications.

In the second phase of the verification, the path conditions are checked to see whether or not they satisfy the property input. For properties $P1$, $M1$, and $S1$ described in Section 4.2, this check completed in 12.72 secs, 1.59 secs, and 5.5 secs, respectively. Overall, none of the 11 multiplicity invariants took more than 2 secs to check, while the verification of the 5 pattern contracts took between 3 and 22 secs. The check of two syntactic invariants completed in less than 6 secs, while the third required 241 secs; the reason is that it is by far the most complex property, with 20 elements distributed over 4 atomic contracts.

#### 4.3.2 Bugs found

To our surprise, SyVOLT determined that the transformation was not correct, because it did not guarantee properties $M1$ and $S1$ (Figs. 7 and 8). More precisely, there are input models for which the transformation generates: (i) an output in which a Par is associated to fewer than two Proc (violating $M1$), and (ii) an output where an Inst named Dispatcher is created but a corresponding ProcDef named Dispatcher is not created (violating $S1$). After examining the generated counter examples, we determined that both bugs were caused by two rules $R1$ and $R2$ in different layers that were not guaranteed to be “applied together”, i.e., that it was possible that $R1$ was applied, but not $R2$.

\(^2\)All timings were done on a 2.8 GHz AMD Opteron processor running Ubuntu Linux.
Neither of these bugs had been exposed by our rule testing while developing the transformation, and when we went back to the the original UML-RT-to-Kiltera transformation in ATL presented in [Pae12], it too, although also having been tested quite thoroughly, turned out to also contain the exact same two bugs.

An investigation of the source of these bugs revealed some details:

1. **Bug 1**: Rule ‘ExitPoint2ProcDef’ in layer 3 (Fig. 9) and rule ‘MapExitWithTrans’ in layer 5 (Fig. 10) are supposed to generate the two Proc elements belonging to a Par element. First, rule ‘ExitPoint2ProcDef’ (Fig. 9) generates a Par element associated to a Trigger element (which extends Proc). Then, rule ‘MapExitWithTrans’ (Fig. 10) associates an Inst element (i.e., a second Proc element) with the same Par element previously generated by rule ‘ExitPoint2ProcDef’ in layer 3, as shown by the free variable ‘parexitpoint’.

   However, execution of rule ‘ExitPoint2ProcDef’ does not mandate execution of rule ‘MapExitWithTrans’; e.g., a composite State in the input model with an ExitPoint that has no outgoing Transitions will cause rule ‘ExitPoint2ProcDef’ (layer 3) to execute but not rule ‘MapExitWithTrans’ in layer 5, resulting in an output containing a Par associated with only one Proc, violating M1.

2. **Bug 2**: Rule ‘MapCompositeState’ in layer 2 generates an Inst named ‘Dispatcher’ and rule ‘State2Dispatcher’ in layer 3 generates a ProcDef named ‘Dispatcher’. Rule ‘State2Dispatcher’ matches composite States with a positive application condition, or a PAC (specified using Exists match elements, described in Section 3.1). On the other hand, rule ‘MapCompositeState’ matches any composite State, without specifying a PAC. Thus, rule ‘MapCompositeState’ will match some composite States that are not matched by rule ‘State2Dispatcher’ (if they do not satisfy the PAC), resulting in an output containing an Inst named Dispatcher, but not a ProcDef named Dispatcher (violating SS2).

### 4.3.3 Fixing the bugs

For the first bug, we merged the two rules ‘ExitPoint2ProcDef’ and ‘MapExitWithTrans’ into a new rule in layer 5. For the second bug, the MatchModel of the rule ‘MapCompositeState’ (layer 2) was updated to include the PAC (specified as Exists match elements) of rule ‘State2Dispatcher’ (layer 3), to guarantee that the two rules necessarily execute together. Due to page limitations, the new rules are not shown here (see [Sel15] for details).

After these changes, our prover proved the revised transformation correct with respect to all 11 properties.

### 5 Observations

Our case study allowed us to make the following observations:

**O1**: “Bugs not triggered by a test input will not be found”: The limits of testing are well-known, of course. However, the unwarranted trust we subconsciously placed in our tests surprised us and highlights the value of formal verification.
O2: “Make sure test inputs cover the input metamodel”: Testing proved insufficient, because the metamodel was assumed to be more restrictive than it actually was, i.e., the input models produced by the prover as counter examples had been assumed to be malformed, but they proved to be permissible UML-RT state machines.

O3: “Effective input-independent verification of graph-based model transformations is possible”: While the performance of an earlier version of our prover [SLC+14] was already quite good, the performance of SyVOLT observed in this non-trivial case study is encouraging and provides additional, albeit still anecdotal, evidence that the formal verification of transformations with respect all possible inputs is feasible and practical.

O4: “Refactoring is hard”: The first bug was introduced by a refactoring step that broke a single rule into the two rules ‘ExitPoint2ProcDef’ and ‘MapExitWithTrans’ described in the previous section. Unfortunately, the refactoring did not preserve correctness and was undone to fix the bug.

O5: “Input/output-level properties” vs “rule-level properties”: The bugs suggested to us that it is useful to distinguish two different kinds of properties: 1) input/output-level properties, i.e., pre- and post-condition-type properties that describe the desired shape of the output (e.g., all properties in Section 4.2); and (2) rule-level properties, i.e., properties that impose restrictions on the way the rules are applied in a transformation execution (e.g., “Rule R1 fires in an execution if and only if rule R2 also fires”). Input/output-level properties capture user-level requirements, while rule-level properties capture when the rules in an implementation work together properly to guarantee the requirements. The relationship is akin to standard pre- and post-conditions for programs (i.e., “contracts”) and, e.g., behavioural interface specification and API method usage rules such as “method close should only be invoked after method open”. The benefit of rule-level properties thus is that they, in some sense, describe how the transformation works and may provide necessary conditions useful for transformation development and documentation.

O6: Towards a development methodology for provably correct DSLTrans transformations: A hallmark of DSLTrans is that transformations are structured in sequentially executed layers $L_1, \ldots, L_n$. The property language supported by SyVOLT is perfectly suited to capture the purpose of each layer $L_{i+1}$ through a pair of formulas $F_i$ and $F_{i+1}$ capturing input/output-level properties, such that the rules in $L_{i+1}$ are deemed correct, if they transform input satisfying the pre-condition $F_i$ into output satisfying the post-condition $F_{i+1}$. Development of the rules in layer $L_{i+1}$ would go hand-in-hand with the development of the formulas $F_{i+1}$ with the iterative use of the prover until (i) the rules are correct with respect to $F_{i+1}$, and (ii) $F_{i+1}$ is considered strong enough to allow the construction of $L_{i+2}$ and a suitable $F_{i+2}$. Failure to establish $F_{i+1}$ may force the developer to revisit a previous level $L_j$ ($j \leq i$) and revise $F_j$ and, possibly, also the rules in $L_j$.

6 Related Work

This paper presents results from our ongoing work on verifying graph-based model transformations. While an earlier version of the prover has been described before [SLC+14], the UML-RT-to-Kiltera case study and our experience verifying it is new to this paper. In a performance comparison in [SBC+13] (using a different case study), our prover performed substantially better than the approach based on satisfiability solving described in [BECG12].

Tools to evaluate the coverage provided by a set of input models with respect to a given metamodel have been proposed [FBMLT09] and may have revealed the limitations of our initial tests. Tools that allow what we call “rule-level properties” include Groove [GdMR+12] and AGG [Tae03]. AGG supports a “critical-pair analysis” which checks if transformation rules are confluent, i.e., applications of different rules to the same graph will produce the same result. Groove’s analysis is more comprehensive and supports a complete exploration of the state space of the transformation; during the exploration a CTL formula is checked in which a atomic proposition captures the applicability of a rule; this way, both input-output- and rule-level properties can be checked.

7 Conclusion and Future Work

The case study has been useful in the following ways: First, it has reinforced some already widely held, but unproven, beliefs (Observations O1, O2, and O4). It provides some additional evidence of the promise of our approach to model transformation verification (Observation O3). Also, it provided us with a stimulus to think more about different kinds of properties; rules form the building blocks transformations are made of and occupy
a higher level of abstraction than, say, statements in programming languages, while also perhaps being more uniform in their effect and role than, say, methods and procedures in programming languages; this may mean that the development of rule-based transformation systems in general and graph-based model transformation systems in particular may benefit greatly from the kind of rule-level properties discussed in Observation O4. Finally, the case study has given us new ideas about how to evolve our work into a transformation system providing suitable tool support for the rigorous development of correct DSLTrans transformations (Observation O5). In particular, support for the expression and verification of properties of individual layers and rule-level properties will be a focus. Encouragingly, it should be fairly straight-forward to extend our prover to support these additions.

References


